# SACRED HEART COLLEGE (AUTONOMOUS) 

Department of Mathematics

MSc Mathematics

Course Plan

2018-19

Semester 4

## COURSE PLAN

| PROGRAMME | M.Sc. MATEMATICS | SEMESTER | 4 |
| :--- | :---: | :---: | :---: |
| COURSE CODE AND TITLE | 16P4MATT16EL : DIFFERENTIAL <br> GEOMETRY | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 75 |
| FACULTY NAME | Dr. DIDIMOS K. V. |  |  |

## Course Objectives

> Perceive ideas of Graphs and level sets, vector fields, the tangent space, surfaces, vector
fields on surfaces, orientation
> Understand the fundamentals of The Gauss map, geodesics, Parallel transport
$>$ Assimilate the ideas of the Weingarten map, curvature of plane curves, Arc length and line integrals
> Developing skills related to Curvature of surfaces

## Text Book

1 Tom Apostol, Mathematical Analysis (second edition), Narosa Publishing House.
2 Walter Rudin, Principles of Mathematical Analysis (Third edition), International Student Edition.

| Sessions | Topic | Method | Remarks |
| :---: | :--- | :--- | :--- |
| 1 | Graphs and level sets | Lecture, Group Discussion, <br> Problem Solving Lecture |  |
| 2 | Graphs and level sets | Lecture, Group Discussion, <br> Problem Solving Lecture |  |
| 3 | vector fields | Lecture, Group Discussion, <br> Problem Solving Lecture |  |
| 4 | vector fields | Lecture, Group Discussion, <br> Problem Solving Lecture |  |
| 5 | The tangent space Group Discussion, |  |  |


|  |  | Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 18 | Vector fields on surfaces, orientation. | Lecture, Group Discussion, Problem Solving |  |
| 19 | Vector fields on surfaces, orientation. | Lecture, Group Discussion, Problem Solving |  |
| 20 | Vector fields on surfaces, orientation. | Lecture, Group Discussion, Problem Solving |  |
| 21 | The Gauss map | Lecture, Group Discussion, Problem Solving |  |
| 22 | The Gauss map | Lecture, Group Discussion, Problem Solving |  |
| 23 | The Gauss map | Lecture, Group Discussion, Problem Solving |  |
| 24 | The Gauss map | Lecture, Group Discussion, Problem Solving |  |
| 25 | Geodesics | Lecture, Group Discussion, Problem Solving |  |
| 26 | Geodesics | Lecture, Group Discussion, Problem Solving |  |
| 27 | Geodesics | Lecture, Group Discussion, Problem Solving |  |
| 28 | Geodesics | Lecture, Group Discussion, Problem Solving |  |
| 29 | Geodesics | Lecture, Group Discussion, Problem Solving |  |
| 30 | Parallel transport | Lecture, Group Discussion, Problem Solving |  |
| 31 | Parallel transport | Lecture, Group Discussion, Problem Solving |  |
| 32 | Parallel transport | Lecture, Group Discussion, Problem Solving |  |
| 33 | Parallel transport | Lecture, Group Discussion, Problem Solving |  |
| 34 | Parallel transport | Lecture, Group Discussion, |  |


|  |  | Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 35 | Parallel transport | Lecture, Group Discussion, Problem Solving |  |
| 36 | The Weingarten map | Lecture, Group Discussion, Problem Solving |  |
| 37 | The Weingarten map | Lecture, Group Discussion, Problem Solving |  |
| 38 | The Weingarten map | Lecture, Group Discussion, Problem Solving |  |
| 39 | The Weingarten map | Lecture, Group Discussion, Problem Solving |  |
| 40 | The Weingarten map | Lecture, Group Discussion, Problem Solving |  |
| 41 | The Weingarten map | Lecture, Group Discussion, Problem Solving |  |
| 42 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 43 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 44 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 45 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 46 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 47 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 48 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 49 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |
| 50 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |
| 51 | Arc length and line integrals | Lecture, Group Discussion, |  |


|  |  | Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 52 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |
| 53 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |
| 54 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |
| 55 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |
| 56 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 57 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 58 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 59 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 60 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 61 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 62 | Curvature of surfaces | Lecture, Group Discussion, Problem Solving |  |
| 63 | Parametrized surfaces | Lecture, Group Discussion, Problem Solving |  |
| 64 | Parametrized surfaces | Lecture, Group Discussion, Problem Solving |  |
| 65 | Parametrized surfaces | Lecture, Group Discussion, Problem Solving |  |
| 66 | Parametrized surfaces | Lecture, Group Discussion, Problem Solving |  |
| 67 | Parametrized surfaces | Lecture, Group Discussion, Problem Solving |  |
| 68 | Parametrized surfaces | Lecture, Group Discussion, |  |


|  |  | Problem Solving |  |
| :---: | :--- | :--- | :--- |
| 69 | Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |
| 70 | local equivalence of <br> surfaces and Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |
| 71 | local equivalence of <br> surfaces and Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |
| 72 | local equivalence of <br> surfaces and Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |
| 73 | local equivalence of | Lecture, Group Discussion, <br> Problem Solving |  |
| 74 | local equivalence of |  |  |
| surfaces and Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |  |
| local equivalence of |  |  |  |
| surfaces and Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |  |

1 ASSIGNMENTS/EXERCISES - Details \& Guidelines

|  | Date of <br> submission/completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :---: | :--- | :--- |
| 1. | 12 March 2019 | Problems on Differential Geometry |

## 2. References:-

1. Serge Lang, Differential Manifolds
2. I.M. Siger, J.A Thorpe, Lecture notes on Elementary topology and Geometry, Springer (1967)
3. S. Sternberg, Lectures on Differential Geometry, Prentice-Hall, 1964.
4. M. DoCarmo, Differential Geometry of curves and surfaces.
5. Goursat, Mathematical Analysis, Vol - 1(last two chapters)

COURSE PLAN

| PROGRAMME | MSc Mathematics | SEMESTER | 4 |
| :---: | :---: | :---: | :---: |
| COURSE CODE AND <br> TITLE | 16P4MATT17EL MULTIVARIATE <br> CALCULUS AND INTEGRAL <br> TRANSFORMS | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 90 |
| FACULTY NAME | SANIL JOSE |  |  |

## Course Objectives

$>$ To Explain Weirstras theorem, otherforms of Fourierseries, the Fourier integral theorem, the exponential form of the Fourier integral theorem, integral transforms and convolutions, the convolution theorem for Fourier transforms.
> To Analyze Multivariable Differential Calculus The directional derivative, directional derivatives and continuity, the total derivative, the total derivative expressed in terms of partial derivatives, An application of complex- valued functions, the matrix of a linear function, the Jacobian matrix, the chain rate matrix form of the chain rule.
$>$ To Interpret Implicit functions and extremum problems, the mean value theorem for differentiable functions, a sufficient condition for differentiability.
$>$ To Explain Integration of Differential Forms, primitive mappings, partitions of unity, change of variables, differential forms, Stokes theorem.

| SESSION | TOPIC | LEARNING RESOURCES | VALUE ADDITIONS | REMARKS |
| :---: | :---: | :---: | :---: | :---: |
| MODULE 1 |  |  |  |  |
| 1 | INTRODUCTION | Lecture |  |  |
| 2 | THE WEIRSTRASS THEOREM | Lecture |  |  |
| 3 | OTHER FORMS OF FOURIER SERIES |  |  |  |
| 4 | THE FOURIER INTEGRAL THEOREM |  |  |  |
| 5 | THE EXPONENTIAL FORM OF FORIER SERIES | Lecture, |  |  |
| 6 | INTEGRAL TRANSFORMS | Lecture Problem Solving |  |  |
| 7 | CONVOLUTION |  |  |  |
| 8 | SEMINAR | Lecture, Problem Solving |  |  |
| 9 | SEMINAR | Lecture, Problem Solving |  |  |
| 10 | PROBLEMS | Lecture, Problem Solving |  |  |
| 11 | PROBLEMS | Lecture, Problem Solving |  |  |
| 12 | TUTORIAL | Lecture |  |  |
| 13 | SEMINAR | Lecture, Problem |  |  |



| 24 | JACOBIAN MATRIX | Lecture, Problem Solving |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 25 | CHAIN RULE MATRIX FORM | Lecture, Problem Solving |  |  |
| 26 | CHAIN RULE MATRIX FORM | Lecture, <br> Problem <br> Solving |  |  |
| 27 | SEMINAR | Lecture, Problem Solving |  |  |
| 28 | SEMINAR | Lecture, <br> Problem <br> Solving |  |  |
| 29 | PROBLEMS |  |  |  |
| 30 | PROBLEMS | Lecture, Problem Solving |  |  |
| 31 | TUTORIAL | Lecture, <br> Problem <br> Solving |  |  |
| 32 | MEAN VALUE THEOREM | Lecture, <br> Problem <br> Solving |  |  |
| 33 | MEAN VALUE THEOREM | Lecture, Problem Solving |  |  |
| 34 | SUCCIFIENT CONDITION FOR DIFFERENTIABILITY | Introduction |  |  |
| 35 | SUCCIFIENT CONDITION FOR DIFFERENTIABILITY | Lecture, Problem Solving |  |  |
| 36 | MIXED DERIVATIVE THEOREM | Lecture, <br> Problem <br> Solving |  |  |
| 37 | INVERSE FUNCTION THEOREM | Lecture, Problem Solving |  |  |
| 38 | IMPLICIT FUNCTION | Lecture, |  |  |


|  | THEOREM | Problem Solving |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 39 | EXTREMA OF REAL VALUED FUNCTIONS |  |  |  |
| 40 | extrema of real valued FUNCTIONS | Lecture, <br> Problem <br> Solving |  |  |
| 41 | SEMINAR | Lecture, Problem Solving |  |  |
| 42 | SEMINAR | Lecture, Problem Solving |  |  |
| 43 | PROBLEMS | Lecture, Problem Solving |  |  |
| 44 | PROBLEMS | Lecture, Problem Solving |  |  |
| 45 | TUTORIAL | Lecture, Problem Solving |  |  |
| 46 | SEMINAR | Lecture, <br> Problem <br> Solving |  |  |
| 47 | SEMINAR | Lecture, Problem Solving |  |  |
| 48 | SEMINAR | Lecture, <br> Problem <br> Solving |  |  |
| 49 | SEMINAR | Lecture, Problem Solving |  |  |
| 50 | SEMINAR | Lecture, <br> Problem <br> Solving |  |  |
| 51 | SEMINAR | Lecture, Problem Solving |  |  |



|  |  | Solving |  |  |
| ---: | :--- | :--- | :--- | :--- |
| 65 | SEMINAR |  | Lecture, <br> Problem <br> Solving |  |
| 66 | SEMINAR | Lecture, <br> Problem <br> Solving |  |  |
| 67 | SEMINAR | Lecture, <br> Problem <br> Solving |  |  |
| 68 | SEMINAR | Lecture, Group <br> Discussion |  |  |
| 69 | SEMINAR | Lecture, Group <br> Discussion |  |  |
| 70 | SEMINAR | Lecture, Group <br> Discussion |  |  |
| 71 | SEMINAR | Lecture, Group <br> Discussion |  |  |
| $72-90$ | SEMINAR | Lecture, Group <br> Discussion |  |  |

INDIVIDUAL ASSIGNMENTS/SEMINAR - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :--- | :--- | :--- |
| 1 | $4 / 1 / 2019$ | Problems from module 1 and 2 |
| 2 | $28 / 1 / 2019$ | Problems from module 4 |

GROUP ASSIGNMENTS/ACTIVITES - Details \& Guidelines

| Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :---: | :---: |
| $2 / 2 / 2019$ | PROBLEMS IN MODULE 3 |

## RECOMMENDED BOOKS:

1. Rudin, W., Principles of Mathematical Analysis, 3rd Edition. New Delhi: McGraw-Hill Inc., 2013.
2. Royden, H.L. and Fitzpatrick, P.M., Real Analysis, 4th Edition. New Delhi: Pearson, 2010.
3. Carothers, N. L., Real Analysis, Cambridge University Press, 2000.
4. Apostol, T.M., Mathematical Analysis -A modern approach to Advanced Calculus. New Delhi: Narosa Publishing House, 1957.
5. Bartle, Robert G. and Sherbert, Donald R., Introduction to Real Analysis, 3rd Edition. Wiley, 1999. 6. Hugh, C.C., Real Mathematical Analysis. Springer, 2003.
6. Abbott, S., Understanding Analysis, 2nd Edition. Springer, 2016
7. Avner Friedman, "Foundations of Modern Analysis", Hold Rinehart Winston, 1970.

9 . Rana I. K., "An Introduction to Measure and Integration", Narosa Publishing House Pvt. Ltd., Second Edition, 2007.

COURSE PLAN

| PROGRAMME | MASTER OF SCIENCE MATHEMATICS | SEMESTER | 4 |
| :---: | :---: | :---: | :---: |
| COURSE CODE AND <br> TITLE | 16P4MATT18EL- COMBINATORICS | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 75 |
| FACULTY NAME | MARIA SEBASTIAN |  |  |

## Course Objectives

> To Analyze permutations and combinations \& its applications.
$>$ To Explain Pigeonhole principle and Ramsey numbers and its applications.
> To Apply generating functions and its implications.
$>$ To Analyze recurrence relation and methods to solve that.

| SESSION | TOPIC | LEARNING <br> RESOURCES | VALUE <br> ADDITIONS | REMARKS |
| :---: | :--- | :--- | :--- | :--- |
| MODULE I |  |  |  |  |
| 1 | Two basic counting principles | PPT |  |  |
| 2 | Problems | Problem solving |  |  |
| 3 | Problems, Permutations | Lecture |  |  |
| 4 | Problems permutations and Principle of | Lecture solving |  |  |
| 5 | Circular problem <br> complementation and problems |  |  |  |
| 6 | Problems, Combinations | Problem solving |  |  |
| 7 | Problems, S(n, r) | Lecture |  |  |
| 8 | Problems, Injection and bijection principle | Lecture |  |  |
| 9 | Problems | Lecture |  |  |
| 10 | Arrangements and problems | Lecture/Problem <br> solving |  |  |


| 11 | Selection with repetitions | Lecture |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 12 | Problems | Lecture/Problem solving |  |  |
| 13 | Distribution problems-different cases | Lecture/Problem solving |  |  |
| 14 | Problems | Lecture |  |  |
| 15 | Extra problems from exercise | Lecture/Problem solving |  |  |
| 16 | Extra problems from exercise | Lecture |  |  |
| 17 | Introduction to binomial coefficients | Lecture/Problem solving |  |  |
| MODULE II |  |  |  |  |
| 18 | Introduction to pigeonhole principle | PPT/Lecture |  |  |
| 19 | Basic problems based on PP | Lecture |  |  |
| 20 | More examples on PP |  |  |  |
| 21 | Problems | Lecture |  |  |
| 22 | Ramsey type problems | Lecture |  |  |
| 23 | More problems and Ramsey numbers | Lecture/Problem solving |  |  |
| 24 | Problems, Generalised Pigeonhole Principle | Lecture/Problem solving |  |  |
| 25 | Theorems on Bounds for Ramsey numbers | Lecture/Problem solving |  |  |
| 26 | Theorems on Bounds for Ramsey numbers | Lecture/Problem solving |  |  |
| 27 | Theorems on Bounds for Ramsey numbers | Lecture/Problem solving |  |  |
| 28 | Problems | Lecture/Problem solving |  |  |
| 29 | Problems | Lecture/Problem solving |  |  |
| 30 | Extra problems from exercise | Lecture/Problem solving |  |  |
|  | CIA-1 |  |  |  |
| 31 | Basic Inclusion and Exclusion principle | Lecture |  |  |
| 32 | Principle of inclusion and exclusion(PIE) and its proof | Lecture/Problem solving |  |  |
| 33 | Problems | Lecture/Problem solving |  |  |
| 34 | Generalisation of PIE and problems | Lecture/Problem solving |  |  |
| 35 | Generalised Principle of inclusion and exclusion(GPIE) and proof | Lecture |  |  |
| 36 | Problems | Lecture/Problem solving |  |  |
| MODULE III |  |  |  |  |
| 37 | Generalised Principle of inclusion and exclusion(GPIE) | Lecture/Problem solving |  |  |
| 38 | Problems | Lecture/Problem |  |  |


|  |  | solving |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 39 | Extra problems from exercise | Lecture/Problem solving |  |  |
| 40 | Shortest route problem | Lecture/Problem solving |  |  |
| 41 | Integer solutions for an equation | Lecture/Problem solving |  |  |
| 42 | More problems | Lecture/Problem solving |  |  |
| 43 | Surjective mappings | Lecture/Problem solving |  |  |
| 44 | Sterling numbers of second kind | Lecture/Problem solving |  |  |
| 45 | Derangements and problems | Lecture/Problem solving |  |  |
| 46 | Generalisation of Derangements | Lecture/Problem solving |  |  |
| 47 | Problems | Lecture/Problem solving |  |  |
| 48 | Test | Lecture/Problem solving |  |  |
| 49 | $\begin{array}{l}\text { Ordinary } \\ \text { product }\end{array}$ generating functions ,Cauchy | Lecture/Problem solving |  |  |
| 50 | Examples | Lecture/Problem solving |  |  |
| 51 | Generating functions for different sequences | Lecture/Problem solving |  |  |
| 52 | Problems | Lecture/Problem solving |  |  |
| 53 | Some modeling problems | Lecture/Problem solving |  |  |
| 54 | Examples | Lecture/Problem solving |  |  |
| Module-IV |  |  |  |  |
| 55 | Partitions of integers | Lecture/Problem solving |  |  |
| 56 | Theorems based on partitions | Lecture/Problem solving |  |  |
| 57 | Ferrers Diagram and problems | Lecture/Problem solving |  |  |
| 58 | Theorems and problems | Lecture/Problem solving |  |  |
| 59 | $\begin{array}{l}\text { Exponential } \\ \text { examples }\end{array}$ generating functions and | Lecture/Problem solving |  |  |
| 60 | Exponential generating functions for permutations and examples | Lecture/Problem solving |  |  |
| 61 | More examples | Lecture/Problem solving |  |  |
| 62 | Distribution problems | Lecture/Problem solving |  |  |


| 63 | Problems from exercise | Lecture/Problem <br> solving |  |  |
| :---: | :--- | :--- | :--- | :--- |
| 64 | Introduction to recurrence relations | Lecture/Problem <br> solving |  |  |
| CIA - II |  |  |  |  |
| 65 | Tower of Hanoi problem | Lecture/Problem <br> solving |  |  |
| 66 | Finding number of parallelograms in the nth <br> sub-division of an equilateral triangle | Lecture/Problem <br> solving |  |  |
| 67 | Method to solve Linear homogenous <br> recurrence relations | Lecture/Problem <br> solving |  |  |
| 68 | Method to solve General Linear recurrence <br> relations | Problem solving |  |  |
| 69 | Number of ways of colouring a circle with n <br> sectors using k colours with certain conditions | Problem solving |  |  |
| 70 | problems | Problem solving |  |  |
| 71 | Finding the determinant of a special type <br> matrix using recurrence relation | Problem solving |  |  |
| $72-75$ | Extra problems | Problem solving |  |  |

INDIVIDUAL ASSIGNMENTS/SEMINAR - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :--- | :---: | :---: |
| 1 | $21 / 12 / 2018$ | PROBLEMS BASED ON MODULE 1 |
| 2 | $15 / 1 / 2019$ | PROBLEMS BASED ON MODULE 2 |

GROUP ASSIGNMENTS/ACTIVITES - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :---: | :---: | :---: |
| 1 | $20 / 2 / 2019$ | Recurrence relations |

## Textbook

CHEN CHUAN-CHONG ,KOH KHEE MENG,PRINCIPLES AND TECHNIQUES IN COMBINATORICS,WORLD SCIENTIFIC,1999.

## References

## Applied Combinatorics

Mitchel T. Keller, Washington and Lee University
William T. Trotter, Georgia Institute of Technology

## Web resource references:

COURSE PLAN

| PROGRAMME | MASTER OF SCIENCE MATHEMATICS | SEMESTER | 4 |
| :---: | :---: | :---: | :---: |
| COURSE CODE AND <br> TITLE | 16P4MATT19EL- THEORY OF <br> WAVELETS | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 75 |
| FACULTY NAME | M P SEBASTIAN |  |  |

## Course Objectives

$>$ Analyze the basics of Wavelet theory.
> Analyze various applications of wavelets
> Apply wavelet theory in Linear algebra.
$>$ Summarize the scope of wavelet theory in the field of medical science.
> Explain the concepts of Haar measure

| SESSION | TOPIC | LEARNING RESOURCES | VALUE ADDITIONS | REMARKS |
| :---: | :---: | :---: | :---: | :---: |
| MODULE I |  |  |  |  |
| 1 | Fundamentals of vector spaces and metric spaces | PPT |  |  |
| 2 | Linear transformations and its matrix representations | Problem solving |  |  |
| 3 | $\mathrm{I}^{2}(\mathrm{~N})$ and $\mathrm{I}^{2}\left(\mathrm{Z}_{\mathrm{N}}\right)$ | Lecture |  |  |
| 4 | Introduction of the orthonormal basis $\left.\mathrm{E}_{2}, \mathrm{E}_{3}, \ldots \ldots . . . ., \mathrm{E}_{\mathrm{N}-1}\right\}$ | Problem solving |  |  |
| 5 | The properties of the above basis | Lecture |  |  |
| 6 | Introduction of the fourier basis F | Problem solving |  |  |
| 7 | Introduction of discrete fourier transform | Lecture |  |  |
| 8 | Matrix representation of the discrete fourier transform | Lecture |  |  |
| 9 | Inverse discrete Fourier transform and its matrix representation | Lecture |  |  |
| 10 | Translation by k operator and its Fourier transform | Lecture/Problem solving |  |  |
| 11 | Conjugate of a vector and its Fourier transform | Lecture |  |  |
| 12 | Translation invariant linear transformation | Lecture/Problem solving |  |  |
| 13 | The result saying that a translation invariant linear transformation is diagonalizable | Lecture/Problem solving |  |  |
| 14 | Convolution of two vectors in $1^{2}\left(Z_{N}\right)$ | Lecture |  |  |
| 15 | Convolution operator and the lemma showing that a convolution operator is translation invarient | Lecture/Problem solving |  |  |


| 16 | The Dirac delta function and its properties | Lecture |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 17 | The DFT of convolution | Lecture/Problem solving |  |  |
| MODULE II |  |  |  |  |
| 18 | Spatially localized and frequency localised bases of $1^{2}\left(Z_{N}\right)$ | PPT/Lecture |  |  |
| 19 | Conjugate reflection and its DFT | Lecture |  |  |
| 20 | Components of a convolution in terms of inner products |  |  |  |
| 21 | The necessary and sufficient condition for $\left\{\mathrm{R}_{\mathrm{k}} \mathrm{W}\right\}$ $\mathrm{k}=0 \mathrm{~N}-1$ to be an orthonormal basis for $\mathrm{I}^{2}\left(Z_{N}\right)$ | Lecture |  |  |
| 22 | Introduction of first stage wavelet basis for $\mathrm{I}^{2}\left(\mathrm{Z}_{\mathrm{N}}\right)$ | Lecture |  |  |
| 23 | Introduction of $z^{*}$ and its DFT | Lecture/Problem solving |  |  |
| 24 | The necessary and sufficient condition for $\left\{\mathrm{R}_{\mathrm{k}} \mathrm{W}\right\}$ ${ }^{\mathrm{M}-1} \mathrm{k}=0$ to be an orthonormal set with M elements | Lecture/Problem solving |  |  |
| 25 | Introduction of the system matrix A( $n$ ) of two vectors $u$ and $v$ | Lecture/Problem solving |  |  |
| 26 | The necessary and sufficient condition for two vectors $u$ and $v$ to generate a first stage wavelet basis for $I^{2}\left(Z_{N}\right)$ | Lecture/Problem solving |  |  |
| 27 | Some examples of first stage wavelet basis | Lecture/Problem solving |  |  |
| 28 | Description of first Shannon basis and first stage real Shannon basis | Lecture/Problem solving |  |  |
| 29 | Introduction with sufficient explanations of first stage Haar basis | Lecture/Problem solving |  |  |
| 30 | Lemma 3.12 | Lecture/Problem solving |  |  |
|  | CIA-1 |  |  |  |
| 31 | Up sampling and down sampling operators and their properties | Lecture |  |  |
| 32 | Introduction of filter bank diagram , its analysis phase and synthesis phase, perfect reconstruction in the filter bank | Lecture/Problem solving |  |  |
| 33 | Lemma 3.15 | Lecture/Problem solving |  |  |
| 34 | The iteration steps in the construction of filter bank diagram | Lecture/Problem solving |  |  |
| 35 | Introduction of $p^{\text {th }}$ stage wavelet filter sequence | Lecture |  |  |
| 36 | The derivation of the output of the $p^{\text {th }}$ stage filter bank using down sampling operators | Lecture/Problem solving |  |  |
| MODULE III |  |  |  |  |
| 37 | The theory used for the reconstruction of the filter bank, the diagram representing the reconstruction phase using up sampling operators | Lecture/Problem solving |  |  |
| 38 | Lemma3.18 | Lecture/Problem solving |  |  |
| 39 | Definition of $\mathrm{D}^{\prime}$ and $\mathrm{U}^{\prime}$ Corollary 3.19 | Lecture/Problem solving |  |  |


| 40 | Introduction of $\mathrm{f}_{\mathrm{l}}, \mathrm{g}_{l}$ Definition 3.20 | Lecture/Problem solving |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 41 | Lemma 3.21 | Lecture/Problem solving |  |  |
| 42 | Lemma 3.22 | Lecture/Problem solving |  |  |
| 43 | Introduction of $\mathrm{p}^{\text {th }}$ stage wavelet basis for ${ }^{2}\left(Z_{N}\right)$ | Lecture/Problem solving |  |  |
| 44 | Lemma3.24 | Lecture/Problem solving |  |  |
| 45 | Orthogonal direct sum of two subspaces of an inner product space and a problem from exercise | Lecture/Problem solving |  |  |
| 46 | Lemma 3.26 | Lecture/Problem solving |  |  |
| 47 | The theorem saying that a $p^{\text {th }}$ stage wavelet filter sequence can produce a $\mathrm{p}^{\text {th }}$ stage wavelet basis . Theorem 3.27 | Lecture/Problem solving |  |  |
| 48 | A new symbolic representation of the $p^{\text {th }}$ stage wavelet basis | Lecture/Problem solving |  |  |
| 49 | The folding lemma | Lecture/Problem solving |  |  |
| 50 | Corollary 3.31 | Lecture/Problem solving |  |  |
| 51 | The $\mathrm{p}^{\text {th }}$ stage Haar system | Lecture/Problem solving |  |  |
| 52 | The $p^{\text {th }}$ stage Shannon wavelet basis for $I^{2}\left(Z_{N}\right)$ | Lecture/Problem solving |  |  |
| 53 | The $\mathrm{p}^{\text {th }}$ stage real Shannon wavelet basis | Lecture/Problem solving |  |  |
| 54 | Daubechies's D6 wavelets on $\mathrm{Z}_{\mathrm{N}}$ | Lecture/Problem solving |  |  |
| Module-IV |  |  |  |  |
| 55 | Definition of Cauchy sequence , Complete inner product space, Hilbert space , symmetric partial sum , the convergence of the series in the form $\sum_{n ⿴ 囗} W$ ( $n$ ) | Lecture/Problem solving |  |  |
| 56 | Definition of $S_{A}$ and $P_{S}(f)$ | Lecture/Problem solving |  |  |
| 57 | Lemma 4.14 | Lecture/Problem solving |  |  |
| 58 | The Hilbert space $\quad L^{2}([-\pi, \pi))$, Cauchy Schwarz inequality and triangle inequality | Lecture/Problem solving |  |  |
| 59 | Introduction of $\quad L^{1}([-\pi, \pi))$, $L^{2}([-\pi, \pi))$ is a proper subset of $[-\pi, \pi))$ | Lecture/Problem solving |  |  |
| 60 | Introduction of the trigonometric system, and proving that it is an orthonormal set | Lecture/Problem solving |  |  |
| 61 | The trigonometric system is complete | Lecture/Problem solving |  |  |
| 62 | Definition 4.23 and corollary 4.24 | Lecture/Problem |  |  |


|  |  | solving |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 63 | Bounded linear transformation between Hilbert spaces and lemma 4.26 | Lecture/Problem solving |  |  |
| 64 | Introduction of translation operator and translation invariant linear transformation | Lecture/Problem solving |  |  |
| CIA - II |  |  |  |  |
| 65 | problems | Lecture/Problem solving |  |  |
| 66 | Theorem 4.28 | Lecture/Problem solving |  |  |
| 67 | FOURIER TRANSFORM , INVERSE FOURIER TRANSFORM and convolution on $I^{2}(Z)$ | Lecture/Problem solving |  |  |
| 68 | Lemma 4.31 | Lecture/Problem solving |  |  |
| 69 | Definition of summable sequences and the normed space $\mathrm{I}^{1}(\mathrm{Z})$ | Lecture/Problem solving |  |  |
| 70 | The translation operator $R_{k}$ and translation invariant linear transformation on $I^{2}(Z),$ example 4.37 | Lecture/Problem solving |  |  |
| 71 | The delta function and lemma 4.39 | Lecture/Problem solving |  |  |
| 72-75 | Problems from exercises | Lecture/Problem solving |  |  |

## INDIVIDUAL ASSIGNMENTS/SEMINAR - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :--- | :---: | :---: |
| 1 | $14 / 12 / 2018$ | PROBLEMS BASED ON MODULE 1 |
| 2 | $14 / 1 / 2019$ | PROBLEMS BASED ON MODULE 2 |

GROUP ASSIGNMENTS/ACTIVITES - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) |
| :---: | :---: | :---: |
| 1 | $12 / 2 / 2019$ | PROBLEMS ON MODULE 4 |

