# SACRED HEART COLLEGE (AUTONOMOUS) 

## Department of Mathematics

M.Sc. Mathematics

## Course plan

Academic Year 2018-19
Semester 2

PROGRAMME OUTCOMES

|  |  |
| :---: | :--- |
| PO 1 | Exercise their critical thinking in creating new knowledge leading to innovation, <br> entrepreneurship and employability. |
| PO 2 | Effectively communicate the knowledge of their study and research in their respective <br> disciplines to their stakeholders and to the society at large. |
| PO 3 | Make choices based on the values upheld by the institution, and have the <br> readiness and know-how to preserve the environment and work towards <br> sustainable growth and development. |
| PO 4 | Develop an ethical view of life and have a broader (global) perspective <br> transcending the provincial outlook. |
| PO5 | Explore new knowledge independently for the development of the nation and the <br> world and are able to engage in a lifelong learning process. |


| PROGRAMME SPECIFIC OUTCOMES |  |
| :--- | :--- |
| PSO1 | Assimilate and analyse advanced concepts in Mathematics. |
| PSO2 | Develop problem-solving skills and apply them independently to solve problems in pure <br> and applied mathematics. |
| PSO3 | Develop skills to mathematically model real-time problems and apply mathematical <br> tools to solve them. |
| PSO4 | Inculcate an aptitude for research. |

COURSE PLAN- ABSTRACT ALGEBRA

| PROGRAMME | Msc Mathematics | SEMESTER | 2 |
| :---: | :---: | :---: | :---: |
| COURSE CODE <br> AND TITLE | 16P2MATTO6:ABSTRACT ALGEBRA | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 90 |
| FACULTY NAME | JEET KURIAN MATTAM |  |  |

COURSE OUTCOMES

| C.O. | C.O. Statement | P.O./P.S.O. | CL | KC | $\begin{aligned} & \text { Class } \\ & \text { Hrs } \end{aligned}$ | Lab Hrs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO1 | Developing ideas of finitely genearted abelian groups, Sylow theorems and applications | P. 0 1/P.S.O 1 | U | C | 26 | 0 |
| CO 2 | Understanding the concept of rings of polynomials, facrorisation of polynomials and ideal structure | P. 0 1/P.S.O 1 | U | C | 33 | 0 |
| CO 3 | Asssimilating the idea of extension fields, algebraic extensions and geometric constructions. | P. 0 1/P.S.O 1 | U | C | 14 | 0 |
| CO4 | Developing ideas of automorphisms of fields, isomorphism extension theorem and Galois theory. | P. 0 1/P.S.O 1 | U | C | 17 | 0 |

CO -PO/PSO Mapping

|  | PO 1 | PO 2 | PO 3 | PO 4 | PO 5 | PO 6 | PSO 1 | PSO 2 | PSO 3 | PSO 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO 1 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 2 | 2 |  |  |  |  |  | 1 |  |  |  |
| CO 3 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 4 | 2 |  |  |  |  |  | 2 |  |  |  |

Mapping Strength
0 - No Mapping strength
1- Low
2- Medium
3- High

Text Book
1.A First Course in Abstract Algebra by John B Fraleigh $3^{\text {rd }}$ Edition

Additional references

1) Contemporary Abstract Algebra by Joseph Gallian
2) Topics in Algebra by I.N.Herstein
3) Algebra by Michael Artin
4) Abstract Algebra by David S Dummit and Richard M Foote.

Proofs of theorems to be avoided in bridge course. Only concept and examples required

| Sessions | Topic | Method | C.O |
| :--- | :--- | :--- | :--- |
| 1 | Bridge Course: Chapter 1 of text | Group Discussion followed <br> by a Lecture session. | C.O1 |
| 2 | Bridge Course : Chapter 2 of text <br> excluding direct products | Interactive <br> including GD | session | C.O1 | Bridge Course: chapter 4 of text. |
| :--- |
| 3 |


| 5 | Bridge Course: Section 27.1-27.20 | Lecture session | C. 01 |
| :---: | :---: | :---: | :---: |
| 5 | Bridge Course: Section 27.1-27.20 | Lecture session | C. 01 |
| 6 <br> MODUL <br> E I <br> BEGINS | Definition 11.1, Theorem 11.2 and example 11.3 | Lecture session | C. 01 |
| 7 | Example 11.4, Theorem 11.5, Corollary 11.6 and example 11.7 | Interactive session and Lecture | C. 01 |
| 8 | Definition 11.8, Theorem 11.9, Example 11.10, Example 11.11 | Lecture | C. 01 |
| 9 | Theorem 11.12, Example 11.13, Definition 11.14, Theorem 11.15 | Lecture | C. 01 |
| 10 | Theorem 11.16, Theorem 11.17 and selected exercises of Exercise 11 | Lecture | C. 01 |
| 11 | Exercise 11 continued | Lecture | C. 01 |


| 12 | Definition 16.1, Example 16.2, Theorem 16.3 | Interactive session | C. 01 |
| :---: | :---: | :---: | :---: |
| 13 | Examples 16.4-16.8 | Assignment and seminar for the students. | C. 01 |
| 14 | Example 16.11, Theorem 16.12, Definition 16.13 and Theorem 16.14 | Lecture | CO1 |
| 15 | Definition 16.15 and theorem 16.16 and example 16.17 | Lecture | C. 01 |
| 16 | Theorem 36.1, Definition 36.2 | Lecture | C. 01 |
| 17 | Theorem 36.3 and Corollary 36.4 | Lecture | C. 01 |
| 18 | Definition 36.5, Lemma 36.6 and Corollary 36.7 | Lecture | C. 01 |
| 19 | The three Sylow Theorems ( Statements only) Example 36.12 and Example 36.13 | Lecture | C. 01 |


| 20 | Theorem 37.1 and definition 37.2 and example 37.3 | Lecture | C. 01 |
| :---: | :---: | :---: | :---: |
| 21 | Theorem 37.4, Lemma 37.5 and Theorem 37.6 | Lecture | C. 01 |
| 22 | Theorem 37.7 and Lemma 37.8 | Lecture | C. 01 |
| 23 | Example 37.9- Example 37.12 | Lecture | C. 01 |
| 24 | Example 37.13-Example 37.15 | Lecture | C. 01 |
| 25 | Examples continued and selected exercises of Exercise 37 | Lecture | C. 01 |
| 26 | FIRST CIA | Written Test; Descriptive. |  |
| 27 <br> MODULE <br> 2 <br> BEGINS | Definition 22.1 and Theorem 22.2 | Lecture | $\mathrm{CO2}$ |
| 28 | Example 22.3, $\mathrm{R}[\mathrm{x}, \mathrm{y}]$, and theorem 22.4 | Lecture | $\mathrm{CO2}$ |


| 29 | Examples 22.6-22.10 | Lecture | CO2 |
| :---: | :---: | :---: | :---: |
| 30 | Theorem 22.11 | Seminar | CO2 |
| 31 | Selected Exercises of Exercise 22 | Seminar | CO 2 |
| 32 | Selected Exercises of Exercise 22 | Seminar | CO2 |
| 33 | Theorem 23.1 |  | C02 |
| 34 | Example 23.2 and Corollary 23.3 | Lecture | CO 2 |
| 35 | Example 23.4 and corollary 23.5 | Lecture | CO 2 |
| 36 | Corollary 23.6, Definition 23.7 and Example 23.8 | Lecture | $\mathrm{CO2}$ |
| 37 | Example 23.9, Theorem 23.10, Theorem 23.11 and Corollary 23.12 | Lecture | $\mathrm{CO2}$ |
| 38 | Example 23.13,23.14 and a similar problem in exercises | Lecture | CO 2 |


| 39 | Theorem 23.15 and example 23.16 | Lecture | C02 |
| :--- | :--- | :--- | :--- |
| 40 | Corollary 23.17 | Lecture | C02 |
| 41 | Definition 27.21, Example <br> $27.22,27.23$ and Theorem 27.24 | Lecture | C02 |
| 42 | Theorem 27.25 and example 27.26 <br> Example 27.26 and theorem 27.27 <br> and selected exercises of exercise <br> 27 | Lecture | Cecture |


| 48 | Example 29.4, 29.5, Definition 29.6,Examples 29.7-29.10. | Lecture | CO 2 |
| :---: | :---: | :---: | :---: |
| 49 | Definition 29.11 and theorem 29.12, Theorem 29.13 | Lecture | CO2 |
| 50 | Definition 29.14, Example 29.15, Simple Extensions | Lecture | CO 2 |
| 51 | Example 29.16, Definition 29.17 and Theorem 29.18 |  | CO 2 |
| 52 | Example 29.19 and selected exercises of Exercise 29 | Lecture | CO2 |
| 53 | selected exercises of Exercise 29 | Seminar | CO2 |
| 54 | $\begin{array}{\|lll\|} \hline \text { Theorem } & 30.23, & \text { Definition } \\ 31.1,31.2 & & \end{array}$ | Lecture | C02 |
| 55 | Theorem 31.3,31.4 | Lecture | C02 |
| 56 | $\begin{array}{\|lll} \text { Corollary } & 31.6,31.7, & \text { Examp;e } \\ 31.8,31.9 \end{array}$ | Lecture | C02 |


| 57 | Example 31.10, Theorem 31.11 | Lecture | CO2 |
| :---: | :---: | :---: | :---: |
| 58 | Theorem 31.12, Corollary 31.13, Definition 31.14 and Theorem 31.15 | Lecture | CO2 |
| 59 | Corollary 31.16, Theorem 31.17 and theorem 31.18 | Lecture | CO 2 |
| 60 | Selected exercises of Exercise 31 |  | CO2 |
| 61MOD ULE III BEGINS | Theorem 32.1 and Corollary 32.5 | Seminar | C03 |
| 62 | Theorem 32.6 | Lecture | C03 |
| 63 | Corollary 32.8, Theorems 32.9- $32.11$ | Seminars | CO 3 |
| 64 | Theorem 33.1, Corollary 33.2, Theorem 33.3 | Lecture | CO 3 |
| 65 | Definition 33.4, Theorem 33.5, Corollary 33.6 and Example 33.7 | Lecture | C03 |


| 66 | Lemma 33.8 and Lemma 33.9 | Lecture | C03 |
| :---: | :---: | :---: | :---: |
| 67 | Theorem 33.10, Corollary 33.11 and Theorem 33.12 |  | CO 3 |
| 68 | Definition 48.1, Example 48.2, Theorem 48.3 | Lecture | C03 |
| 69 | Corollary 48.5, Corollary 48.6 and Example 48.7 | Lecture | CO 3 |
| 70 | Definition 48.8, Example 48.9, 48.10, 48.11 and Definition 48.12 | Lecture | CO 3 |
| 71 | Example 48.13, Theorem 48.14, Theorem 48.15, Definition 48.16, Example 48.17 |  | CO 3 |
| 72 | Theorem 48.19, Selected Exercises of Exercise 48 |  | CO 3 |
| 73 | Theorem 49.3( Statement only) and Corollary 49.5 |  | CO 3 |
| 74 | SECOND CIA |  | CO 3 |


| 75 <br> MODUL <br> E IV <br> BEGINS | Definition 50.1, Example 50.2, Theorem $50.3$ | Lecture | CO4 |
| :---: | :---: | :---: | :---: |
| 76 | Definition 50.4, Example 50.5, Corollary 50.6, 50.7 | Lecture | $\mathrm{CO4}$ |
| 77 | Example 50.8 and 50.9. Selected Exercises of Exercise 50. | Lecture | $\mathrm{CO4}$ |
| 78 | Definition 51.1, Theorem 51.2, Corollary 51.3. | Lecture | $\mathrm{CO4}$ |
| 79 | Example 51.4, Theorem 51.6, Definition <br> 51.7 and Example 51.8 | Lecture | CO4 |
| 80 | Theorem 51.9 and Corollary 51.10 | LECTURE | C04 |
| 81 | Lemma 51.11, Definition 51.12 and Theorem 51.13 | LECTURE | $\mathrm{CO4}$ |
| 82 | Theorem 51.14 | LECTURE | CO4 |
| 83 | Theorem 51.15 | LECTURE | C04 |


| 84 | Definition 53.1, Theorem 53.2 | LECTURE | C04 |
| :--- | :--- | :--- | :--- |
| 85 | Example 53.3, Definition 53.5 | LECTURE | C04 |
| 86 | Theorem 53.6 | LECTURE | C04 |
| 87 | Theorem 53.6 (Continued) | LECTURE | C04 |
| 88 | Theorem 53.7 and Example 53.8 | LECTURE | C04 |
| 89 | REVISION |  |  |
| 90 | REVISION |  |  |

COURSE PLAN- ADVANCED TOPOLOGY

| PROGRAMME | Msc Mathematics | SEMESTER | 1 |
| :---: | :---: | :---: | :---: |
| COURSE CODE <br> AND TITLE | 16P2MATTO7: ADVANCED TOPOLOGY | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 75 |
| FACULTY NAME | JEENU KURIAN |  |  |


| CO | CO Statement | PO/PSO | CL | KC | Class Hrs. |
| :--- | :--- | :--- | :--- | :--- | :--- |
| CO1 | Understand Urysohn Characterization <br> of Normality, ,Tietze Characterization <br> of <br> Normality, Products and co-products. | PO1/PSO 1 | U | C | 21 |
| CO2 | Analyze embedding and Metrisation, <br> Evaluation Functions in to Products, <br> embedding Lemma and Tychnoff <br> Embedding, The Urysohn Metrisation <br> Theorem. | PO1/PSO 1 | U | P | 12 |
| CO3 | Develop the idea of convergence and <br> related properties of nets and filters. | PO1/PSO 1 | U | C | 21 |
| CO4 | Understand compactness, <br> variations of compactness. | PO1/PSO 1 | U | C | 21 |

CO -PO/PSO Mapping

|  | PO 1 | PO 2 | PO 3 | PO 4 | PO 5 | PO 6 | PSO 1 | PSO 2 | PSO 3 | PSO 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO 1 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 2 | 2 |  |  |  |  |  | 1 |  |  |  |
| CO 3 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 4 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 5 | 2 |  |  |  |  |  | 2 |  |  |  |

## Mapping Strength

0 - No Mapping strength
1- Low
2- Medium
3- High

| Sessions | Topic | Method | Course Outcome |
| :---: | :---: | :---: | :---: |
| 1. | Introductory Session - separation axioms | Lecture | CO1 |
| 2. | Urysohn characterisation of normality | Lecture | CO1 |
| 3. | Definition and proposition | Lecture | CO1 |
| 4. | Urysohn's Lemma | Lecture, | CO1 |
| 5. | Theorem and Lemma | Lecture, | CO1 |
| 6. | Theorems and Lemma | Lecture, | CO1 |
| 7. | Tietz characterisation of normality: proposition | Lecture, | CO1 |


|  | Proposition | Lecture, |  | CO1 |
| :---: | :---: | :---: | :---: | :---: |
| 9. | Definition and proposition | Lecture, |  | CO1 |
| 10. | Proposition | Lecture |  | CO1 |
| 11. | Theorem and proposition | Lecture, |  | CO1 |
| 12. | Products and co products Cartesian products of family of sets: Basic definitions | Lecture |  | CO1 |
| 13. | Proposition | Lecture, |  | CO1 |
| 14. | Proposition | Lecture, |  | CO1 |
| 15. | Theorem | Lecture, |  | CO1 |
| 16. | Theorem | Lecture, |  | CO1 |
| 17. | Definition and Theorem | Lecture, |  | CO1 |
| 18. | Product topology - Basic definitions | Lecture, Discussion, Solving | Group Problem | CO1 |
| 19. | Theorems | Lecture, |  | CO1 |




| 42 | Theorems and proposition | Lecture, | CO3 |
| :---: | :---: | :---: | :---: |
| 43. | Topology and convergence of nets - Basic definitions | Lecture, | CO3 |
| 44. | Theorems and corollaries | Lecture, | CO3 |
| 45. | Theorems and corollaries | Lecture, | CO3 |
| 46. | Theorems and Propositions | Lecture, | CO3 |
| 47. | Theorems and propositions | Lecture, | CO3 |
| 48. | Filters and their convergence Basic definitions | Lecture, | CO3 |
| 49. | Theorems and corollaries | Lecture, | CO3 |
| 50. | Theorems and Propositions | Lecture, | CO3 |
| 51. | Theorems and Propositions | Lecture, | CO3 |
| 52. | Ultrafilter and compactness | Lecture, | CO3 |
| 53. | Ultrafilter and compactness | Lecture, | CO3 |
| 54. | Theorems and propositions | Lecture, | CO3 |
| 55. | Problems | Lecture, | CO3 |


| 56. | Module 4 - Introduction | Lecture | CO4 |
| :---: | :---: | :---: | :---: |
| 57. | Variation of compactness - Basic definitions | Lecture, | CO4 |
| 58. | Theorems, corollaries and propositions | Lecture, | CO4 |
| 59. | Theorems, corollaries and propositions | Lecture, | CO4 |
| 60. | Theorems, corollaries and propositions | Lecture, | CO4 |
| 61. | Theorems, corollaries and propositions | Lecture, | CO4 |
| 62. | Theorems, corollaries and propositions | Lecture, | CO4 |
| 63. | Local compactness - Definitions | Lecture, | CO4 |
| 64. | Propositions and corollaries | Lecture, | CO4 |
| 65. | Propositions and corollaries | Lecture, | CO4 |
| 66. | Propositions and corollaries | Lecture, | CO4 |
| 67. | Compactification- Basic definitions | Lecture, | CO4 |


| 68. | Theorems and proposition | Lecture, | CO4 |
| :---: | :---: | :---: | :---: |
| 69. | Propositions and corollaries | Lecture, | CO4 |
| 70. | Theorems | Lecture, | CO4 |
| 71. | Theorems | Lecture, | CO4 |
| 72. | Propositions | Lecture, | CO4 |
| 73. | Propositions | Lecture, | CO4 |
| 74. | Problems | Group discussion | CO4 |
| 75. | Problems | Group discussion | CO4 |
| 76. | Problems | Group discussion | CO4 |
| 77. | Problems | Group discussion | CO4 |
| 78. | Problems | Group discussion | CO4 |

INDIVIDUAL ASSIGNMENTS/SEMINAR - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - <br> Graded or Non-graded etc) | Course <br> Outcome |
| :---: | :---: | :---: | :---: |
| 1 | $10^{\text {th }}$ Jan 2019 | Assisgnment product topology, Nets and Filters | CO1, CO3 |

## References:

1. Munkers J.R, Topology - A first course, Prentice Hall of India Pvt.Ltd., New Delhi,2000.
2. J.L.Kelly, General Topology.Van Nostrand, Reinhold Co.,NewYork,1995.
3. Stephen Willard, General Topology,Addison - Wesley.
4. Dugundji, Topology, Universal Book Stall, New Delhi.
5. George F Simmons, introduction to Topology and Modern Analysis, Mc Graw-Hill Book Company,1963.

| PROGRAMME | MSC MATHEMATICS | SEMESTER | 2 |
| :---: | :---: | :---: | :---: |
| COURSE CODE <br> AND TITLE | 16P2MATTO8: ADVANCED COMPLEX <br> ANALYSIS | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 72 |
| FACULTY NAME | PROF. SANIL JOSE |  |  |

## Course Prerequisites:

Calculus, Analysis
Guidelines/Suggestions for Teaching Methods and Student Learning Activities:
This course is taught as a lecture course with student participation and use of computers

| COURSE OUTCOMES |  | PO /PSO |
| :--- | :--- | :--- |
| CO 1 | Understand the concepts of power series to expand a <br> complex function as Taylors and Laurantz series | PO1, PSO1 |
| CO 2 | Perceive entire functions, Jensen's formula, the genus and <br> order of an entire function, Hadamard Factorization <br> theorem. | PO1, PSO1 |
| CO 3 | Interpret Harmonic functions, Basic properties of harmonic <br> functions and Harmonic functions on the disk and discuss <br> Reiman Mapping theorem | PO1, PSO1 |
| CO 4 | Analysis Elliptic functions and Weistrass function | PO1, PSO1 |

CO -PO/PSO Mapping

|  | PO 1 | PO 2 | PO 3 | PO 4 | PO 5 | PO 6 | PSO 1 | PSO 2 | PSO 3 | PSO 4 |
| :--- | :---: | :--- | :--- | :--- | :--- | :--- | ---: | :--- | :--- | :--- |
| CO 1 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 2 | 2 |  |  |  |  |  | 1 |  |  |  |
| CO 3 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 4 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 5 | 2 |  |  |  |  |  | 2 |  |  |  |

## Mapping Strength

0 - No Mapping strength
1- Low
2- Medium
3- High

## Basic Reference

1. AHLFORS V. LARS, COMPLEX ANALYSIS, McGRAW- HILL INTERNATIONAL EDITIONS, $3^{\text {RD }}$ EDITION Hour wise planning

| Sessions | Topic | Method | VALUE ADDITIONS |
| ---: | :--- | :--- | :--- |
| 1 | INTRODUCTION |  |  |
| 2 | ELEMENTARY THEORY OF <br> POWER SERIES |  | CO 1 |
| 3 | SEQUENCE AND SERIES |  | CO 1 |
| 4 | UNIFORM CONVERGANCE |  | CO 1 |
| 5 | POWER SERIES 1 |  |  |
| 6 | ABEL'S LIMIT THEOREM |  | CO 1 |


| 7 | POWER SERIES EXPNSION | CO 1 |
| :---: | :---: | :---: |
| 8 | WEISTRASS THEOREM | CO 1 |
| 9 | TAYLOR'S THEOREM | CO 1 |
| 10 | LAURENT'S THEOREM | CO 1 |
| 11 | PARTIAL FRACTIONS | CO 1 |
| 12 | INFINITE PRODUCTS | CO 1 |
| 13 | CANNONICAL PRODUCTS | CO 1 |
| 14 | GAMMA FUNCTION | CO 1 |
| 15 | GAMMA FUNCTION | CO 1 |
| 16 | SEMINAR | CO 1 |
| 17 | SEMINAR/ PROBLEM DISCUSSION | CO 1 |
| 18 | SEMINAR/ PROBLEM DISCUSSION | CO 1 |
| 19 | SEMINAR/ PROBLEM DISCUSSION | CO 1 |
| 20 | SEMINAR/ PROBLEM | CO 1 |


|  | DISCUSSION |  |
| :---: | :---: | :---: |
| 21 | JENSON'S FORMULA | CO 2 |
| 22 | HADAMARD'S THEOREM | CO 2 |
| 23 | THE REIMANN ZETAFUNCTION | CO 2 |
| 24 | EXTENSION TO THE ENTIRE PLANE | CO 2 |
| 25 | FUNCTIONLA EQUATION | CO 2 |
| 26 | THE ZEROS OF ZETA FUNCTION | CO 2 |
| 27 | THE ZEROS OF ZETA FUNCTION | CO 2 |
| 28 | THE ZEROS OF ZETA FUNCTION | CO 2 |
| 29 | ARZELA'S THEOREM | CO 2 |
| 30 | ARZELA'S THEOREM | CO 2 |
| 31 | SEMINAR | CO 2 |
| 32 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| 33 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |


| 34 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| :---: | :---: | :---: |
| 35 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| 36 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| 37 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| 38 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| 39 | SEMINAR/ PROBLEM DISCUSSION | CO 2 |
| 40 | THEREIMANN MAPPING THEOREM | CO 3 |
| 41 | THEREIMANN MAPPING THEOREM | CO 3 |
| 42 | THEREIMANN MAPPING THEOREM | CO 3 |
| 43 | BOUNDARY BEHAVIOUR | CO 3 |
| 44 | USE OF REFLECTION PRINCIPLE | CO 3 |
| 45 | ANALYTIC ARCS | CO 3 |


| 46 | CONFORMAL MAPPING OF POLYGONS | CO 3 |
| :---: | :---: | :---: |
| 47 | SCHWARZ CHRISTOFFEL FORMULA | CO 3 |
| 48 | MEAN VALUE PROPERTY | CO 3 |
| 49 | MEAN VALUE PROPERTY | CO 3 |
| 50 | HARNACK'S PRINCIPLE | CO 3 |
| 51 | HARNACK'S PRINCIPLE | CO 3 |
| 52 | HARNACK'S PRINCIPLE | CO 3 |
| 53 | SUBHARMONIC FUNCTIONS | CO 3 |
| 54 | SUBHARMONIC FUNCTIONS | CO 3 |
| 55 | SEMINAR/ PROBLEM DISCUSSION | CO 3 |
| 56 | SEMINAR/ PROBLEM DISCUSSION | CO 3 |
| 57 | SEMINAR/ PROBLEM DISCUSSION | CO 3 |
| 58 | SEMINAR/ PROBLEM DISCUSSION | CO 3 |


| 59 | SEMINAR/ PROBLEM DISCUSSION | CO 3 |
| :---: | :---: | :---: |
| 60 | SEMINAR/ PROBLEM DISCUSSION | CO 3 |
| 61 | SIMPLY PERIODIC FUNCTIONS | CO 4 |
| 62 | DOUBLY PERIODIC FUNCTIONS | CO 4 |
| 63 | THE FOURIER DEVELOPMENT | CO 4 |
| 64 | THE PERIOD MODULE | CO 4 |
| 65 | UNIMODULAR TRANSFORMATIONS | CO 4 |
| 66 | CANNONICAL BASIS | CO 4 |
| 67 | WEISTRASS FUNCTION | CO 4 |
| 68 | WEISTRASS FUNCTION | CO 4 |
| 69 | WEISTRASS FUNCTION | CO 4 |
| 70 | WEISTRASS FUNCTION | CO 4 |
| 71 | SEMINAR/ PROBLEM DISCUSSION | CO 4 |


| 72 | SEMINAR/ PROBLEM <br> DISCUSSION |  | CO 4 |
| ---: | :--- | :--- | :--- |
| 73 | SEMINAR/ PROBLEM <br> DISCUSSION | CO 4 |  |
| 74 | SEMINAR/ PROBLEM <br> DISCUSSION |  | CO 4 |
| 75 | SEMISCUSSION |  | CO 4 |
| 76 | SEMINAR/ PROBLEM <br> DISCUSSION |  | CO 4 |
| 77 | REVISION |  | CO 4 |
| 78 | REVISION |  | CO 4 |

INDIVIDUAL ASSIGNMENTS/SEMINAR - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of <br> assignment (Individual/Group - <br> Written/Presentation - Graded or Non- <br> graded etc) | Course <br> Outcome |
| :---: | :---: | :---: | :---: |
| 1 | $4 / 1 / 2019$ | PROBLEMS ON POWER SERIES | CO 1 |
| 2 | $28 / 1 / 2019$ | PROBLEMS IN HARMONIC FUNCTIONS | CO 3 |

GROUP ASSIGNMENTS/ACTIVITES - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - Graded <br> or Non-graded etc) | Course <br> Outcome |
| :---: | :---: | :--- | :---: |
| $\mathbf{1}$ | $2 / 2 / 2019$ | PROBLEMS IN ELLIPTIC FUNCTIONS | CO 4 |
| $\mathbf{2}$ | $9 / 2 / 2019$ | PROBLEMS IN MODULE 2 | CO 2 |

## References:

1. John. B. Conway, Functions of Complex Variables, SpringerVerlag, New York, 1973. (Indian Edition: Narosa)
2. S. Lang, Complex Analysis, McGraw Hill (1998).
3. S. Ponnusamy \& H. Silverman, Complex Variables with Applications, Birkhauser
4. A. Priestley, Introduction to Complex Analysis, Oxford University Press Tristan Needham, Visual Complex Analysis, Oxford University Press(1999)
5. V. Karunakaran, Complex Analysis, Narosa Publishing House,

| Course | FUNCTIONAL ANALYSIS |
| :--- | :--- |
| Course code | 16P2MATTO9 |
| Semester | 2 |
| Total hours | 75 |
| Credits | 4 |
| Faculty | Prof. M P Sebastian |

## Course Outcomes

| CO1 | Understand the basics of Functional analysis | PO1, PSO1 |
| :--- | :--- | :--- |
| CO2 | Apply Functional analysis in the other disciplines. | PO1, PSO1 |
| CO3 | Understand theory of Operators and Functionals using <br> Linear Algebra. | PO1, PSO1 |
| CO4 | Discover the link of Functional analysis with geometry, <br> differential equations etc. | PO1, PSO1 |

CO -PO/PSO Mapping

|  | PO 1 | PO 2 | PO 3 | PO 4 | PO 5 | PO 6 | PSO 1 | PSO 2 | PSO 3 | PSO 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO 1 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 2 | 2 |  |  |  |  |  | 1 |  |  |  |
| CO 3 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 4 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 5 | 2 |  |  |  |  |  | 2 |  |  |  |

## Mapping Strength

0 - No Mapping strength
1- Low
2- Medium
3- High

| SI.No | No. of <br> Session <br> s/hrs | Topics to be taught | Method of <br> teaching | co | Value <br> addition |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | Fundamentals of Linear Algebra and <br> Metric spaces. | Lecture, <br> Seminar, <br> Assignment | CO3,CO1 |  |
| 2. | 3 | Normed space and Banachspace, <br> examples and their properties, <br> problems. | Lecture, <br> assignment | CO1,CO3 |  |
| 3 | 2 | Finite dimensional normed spaces <br> and their sub spaces, problems. | Lecture | CO1,CO3 |  |
| 4 | 2 | Compactness and finite dimension, <br> problems. | Lecture | CO1,CO3 |  |
| 5 | 2 | Linear operators, examples and <br> their properties, problems. | Lecture, <br> assignment | CO1, <br> CO2,CO3 |  |
| 6 |  | Test paper. |  |  |  |


| 7 | 2 | Bounded and continuous linear operators and examples. | Lecture | $\begin{aligned} & \mathrm{CO} 1, \mathrm{CO} 2, \\ & \mathrm{CO} 4 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| 8 | 2 | Problems based on bounded linear operators. | Lecture | $\begin{aligned} & \mathrm{CO} 1, \mathrm{CO} 3, \\ & \mathrm{CO} 4 \end{aligned}$ |
| 9 | 1 | Linear functionals, examples. | Lecture | CO1, CO3 |
| 10 |  | First internal |  |  |
| 11 | 2 | Bounded linear Functionals and their properties, problems. | Lecture | $\begin{aligned} & \mathrm{CO1}, \\ & \mathrm{CO3,CO4} \end{aligned}$ |
| 12 | 2 | Linear Operators andFunctionals on a finite dimensional normed space, problems. | Lecture, assignment | $\begin{aligned} & \mathrm{CO} 1, \mathrm{CO} 2 \\ & \text {,CO3 } \end{aligned}$ |
| 13 | 2 | Normed space of Operators and Functionals. | Lecture, assignment | $\begin{aligned} & \text { CO1, CO2 } \\ & \text {,CO3 } \end{aligned}$ |
| 14 | 2 | Examples of dual spaces. | Lecture | $\begin{aligned} & \mathrm{CO} 1, \mathrm{CO} 2, \\ & \mathrm{CO} 3 \end{aligned}$ |
| 15 |  | Test paper on module 2 |  |  |
| 16 | 2 | Inner product spaces and Hilbert spaces, examples, problems. | Lecture | $\begin{aligned} & \mathrm{CO} 2, \mathrm{CO} 3, \\ & \mathrm{CO} 4 \end{aligned}$ |
| 17 | 2 | Further properties of inner product spaces. | Lecture , seminar | CO2, CO4 |
| 18 | 2 | Orthogonal complement and direct | Lecture | CO2, CO3 |


|  |  | sum, problems. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 | 2 | Orthogonal sets and sequences. | seminar | $\begin{aligned} & \mathrm{CO}, \mathrm{CO} 3, \\ & \mathrm{CO} 4 \end{aligned}$ |  |
| 20 | 2 | Bessel inequality, Gram- Schmidt process for ortho normalisation. | Lecture, seminar | $\mathrm{CO} 2, \mathrm{CO} 3$ |  |
| 21 | 2 | Total ortho normal sets and sequences , problems. | Lecture, seminar, assignment | $\begin{aligned} & \mathrm{CO} 2, \mathrm{CO} 3 \\ & \mathrm{CO} 4 \end{aligned}$ |  |
| 22 | 2 | Rieszs theorem. | seminar | CO2, CO3 |  |
| 23 | 2 | Sesqui linear functional and Riesz representation theorem. | Lecture, seminar | CO2, CO3 |  |
| 24 | 3 | Problems based on Riesz theorem and Riesz representation theorem. | Lecture | $\mathrm{CO} 2, \mathrm{CO} 3$ |  |
| 25 | 3 | Hilbert adjoint and its properties. | Lecture, seminar | $\begin{aligned} & \mathrm{CO} 2, \mathrm{CO} 3 \\ & \text {,CO4 } \end{aligned}$ |  |
| 2 | 3 | Problems based on Hilbert adjoint operators. | Lecture, assignment , seminar | $\begin{aligned} & \mathrm{CO}, \mathrm{CO} 3, \\ & \mathrm{CO} 4 \end{aligned}$ |  |
| 27 | 3 | Self adjoint, normal and unitary operators, problems. | Lecture, assignment | CO1, CO2 |  |
| 28 |  | Test paper on module 3. |  |  |  |

$\left.\begin{array}{|l|l|l|l|l|l|}\hline 29 & 2 & \text { Zorns Lemma and its applications. } & \text { Lecture } & \text { CO1, CO3 } & \\ \hline 30 & 2 & \begin{array}{l}\text { Hahn Banach theorem for real vector } \\ \text { space. }\end{array} & \text { Lecture } & \text { CO1, CO2, } \\ \text { CO3 }\end{array}\right]$.

INDIVIDUAL ASSIGNMENTS/SEMINAR - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of assignment <br> (Individual/Group - Written/Presentation - Graded <br> or Non-graded etc) | Course <br> Outcome |
| :---: | :---: | :--- | :---: |
| 1 | $2 / 1 / 2019$ | PROBLEMS FROM MODULE 1 | CO 1 |
| 2 | $29 / 1 / 2019$ | PROBLEMS FROM MODULE 2 | CO 2 |

GROUP ASSIGNMENTS/ACTIVITES - Details \& Guidelines

|  | Date of <br> completion | Topic of Assignment \& Nature of <br> assignment (Individual/Group - <br> Written/Presentation - Graded or Non- <br> graded etc) | Course <br> Outcome |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $5 / 2 / 2019$ | PROBLEMS FROM MODULE-4 | CO 3 |

Text book : Introductory Functional Analysis with applications
AUTHOR: ERWIN KREYSZIG, Wiley Classic Library Edition Published 1989
REFERENCES: i) DAY M M , normed linear spaces $3^{\text {rd }}$ edn
ii) TAYLOR A E, introduction to functional analysis

COURSE PLAN-REAL ANALYSIS

| PROGRAMME | M.Sc. MATEMATICS | SEMESTER | 2 |
| :--- | :---: | :---: | :---: |
| COURSE CODE AND <br> TITLE | 16P2MATT10: REAL ANALYSIS | CREDIT | 4 |
| HOURS/WEEK | 5 | HOURS/SEM | 75 |
| FACULTY NAME | Dr. DIDIMOS K. V. |  |  |


| CO | CO Statement | PO/PSO | CL | KC | Class <br> Hrs. | Lab <br> Hrs. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| CO1 | Studying functions of bounded <br> variations, rectifiable curves, <br> paths and equivalence of <br> paths. | PO1/PSO 1 | U | C | 12 | 0 |
| CO2 | Developing the ideas of <br> Riemann-Stieljes integral and <br> studying integration and <br> differentiation. | PO1/PSO 1 | U | C | 25 | 0 |
| CO3 | Assimilating the ideas of <br> uniform convergence and <br> continuity, uniform <br> convergence and integration, <br> uniform convergence and <br> differentiation. | PO1/PSO 1 | U | C | 15 | 0 |
| CO4 | Analysing power series, <br> exponential and trigonometric <br> functions. | PO1/PSO 1 | U C | 23 | 0 |  |

CO -PO/PSO Mapping

|  | PO 1 | PO 2 | PO 3 | PO 4 | PO 5 | PO 6 | PSO 1 | PSO 2 | PSO 3 | PSO 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO 1 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 2 | 2 |  |  |  |  |  | 1 |  |  |  |
| CO 3 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 4 | 2 |  |  |  |  |  | 2 |  |  |  |
| CO 5 | 2 |  |  |  |  |  | 2 |  |  |  |

Mapping Strength
0 - No Mapping strength
1- Low
2- Medium
3- High

| No of Hours | Topic | Method | Course Outcome |
| :---: | :---: | :---: | :---: |
| 1 | A quick review on continuity, uniform continuity, convergence of sequence and series. | Lecture, Group Discussion, Problem Solving Lecture | $\begin{aligned} & \mathrm{CO} / \mathrm{l} \\ & \mathrm{CO} / \\ & \mathrm{CO} / \\ & \mathrm{CO} 4 \end{aligned}$ |
| 2 | A quick review on continuity, uniform continuity, convergence of sequence and series. | Lecture, Group Discussion, Problem Solving Lecture | $\begin{aligned} & \mathrm{CO} / \mathrm{l} \\ & \mathrm{CO} / \mathrm{I} \\ & \mathrm{CO} / \\ & \mathrm{CO} 4 \end{aligned}$ |
| 3 | A quick review on continuity, uniform continuity, convergence of sequence and series. | Lecture, Group Discussion, Problem Solving Lecture | $\begin{aligned} & \mathrm{CO} / \mathrm{l} \\ & \mathrm{CO} / \\ & \mathrm{CO} / \\ & \mathrm{CO} 4 \end{aligned}$ |


| 4 | A quick review on continuity, uniform continuity, convergence of sequence and series. | Lecture, Group Discussion, Problem Solving Lecture | $\begin{aligned} & \mathrm{CO} / \mathrm{l} \\ & \mathrm{CO} / 2 \\ & \mathrm{CO} / \\ & \mathrm{CO} / \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 5 | A quick review on continuity, uniform continuity, convergence of sequence and series. | Lecture, Group Discussion, Problem Solving Lecture | $\begin{aligned} & \mathrm{CO} / \mathrm{l} \\ & \mathrm{CO} / \mathrm{I} \\ & \mathrm{CO} / \\ & \mathrm{CO} 4 \end{aligned}$ |
| 6 | Introduction properties of monotonic functions | Lecture, Group Discussion, Problem Solving | CO1 |
| 7 | Introduction properties of monotonic functions | Lecture, Group Discussion, Problem Solving | CO1 |
| 8 | functions of bounded variation | Lecture, Group Discussion, Problem Solving | CO1 |
| 9 | functions of bounded variation | Lecture, Group Discussion, Problem Solving | CO1 |
| 10 | total variation | Lecture, Group Discussion, Problem Solving | CO1 |
| 11 | total variation | Lecture, Group Discussion, Problem Solving | CO1 |
| 12 | additive property of total variation | Lecture, Group Discussion, Problem Solving | CO1 |


| 13 | additive property of total variation | Lecture, Group Problem Solving | Discussion, | CO1 |
| :---: | :---: | :---: | :---: | :---: |
| 14 | total variation on $(\mathrm{a}, \mathrm{x})$ as a functions of $x$ | Lecture, Group Problem Solving | Discussion, | CO1 |
| 15 | total variation on ( $\mathrm{a}, \mathrm{x}$ ) as a functions of $x$ | Lecture, Group Problem Solving | Discussion, | CO1 |
| 16 | functions of bounded variation expressed as the difference of increasing functions | Lecture, Group Problem Solving | Discussion, | CO1 |
| 17 | functions of bounded variation expressed as the difference of increasing functions | Lecture, Group Problem Solving | Discussion, | CO1 |
| 18 | continuous functions of bounded variation | Lecture, Group Problem Solving | Discussion, | CO1 |
| 19 | continuous functions of bounded variation | Lecture, Group Problem Solving | Discussion, | CO1 |
| 20 | curves and paths | Lecture, Group Problem Solving | Discussion, | CO1 |
| 21 | curves and paths | Lecture, Group Problem Solving | Discussion, | CO1 |
| 22 | rectifiable path and arc length | Lecture, Group Problem Solving | Discussion, | CO1 |


| 23 | rectifiable path and arc length | Lecture, Group Problem Solving | Discussion, | CO1 |
| :---: | :---: | :---: | :---: | :---: |
| 24 | additive and continuity properties of arc length | Lecture, Group Problem Solving | Discussion, | CO1 |
| 25 | equivalence of paths | Lecture, Group Problem Solving | Discussion, | CO1 |
| 26 | Definition and existence of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 27 | Definition and existence of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 28 | Definition and existence of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 29 | Definition and existence of the integral | Lecture, Group Problem Solving | Discussion, | CO2 |
| 30 | Definition and existence of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 31 | properties of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 32 | properties of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 33 | properties of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |


| 34 | properties of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| :---: | :---: | :---: | :---: | :---: |
| 35 | properties of the integral | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 36 | Integration and differentiation | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 37 | Integration and differentiation | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 38 | Integration and differentiation | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 39 | Integration and differentiation | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 40 | Integration and differentiation | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 41 | integration of vector valued functions | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 42 | integration of vector valued functions | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 43 | integration of vector valued functions | Lecture, Group Problem Solving | Discussion, | CO 2 |
| 44 | integration of vector valued functions | Lecture, Group Problem Solving | Discussion, | CO 2 |


| 45 | integration of vector valued functions | Lecture, Group Problem Solving | Discussion, | CO 2 |
| :---: | :---: | :---: | :---: | :---: |
| 46 | Discussion of main problem | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 47 | Discussion of main problem | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 48 | uniform convergence | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 49 | uniform convergence | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 50 | uniform convergence | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 51 | uniform convergence | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 52 | uniform convergence | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 53 | uniform convergence | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 54 | uniform convergence and continuity | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 55 | uniform convergence and continuity | Lecture, Group Problem Solving | Discussion, | CO 3 |


| 56 | uniform convergence and continuity | Lecture, Group Problem Solving | Discussion, | CO3 |
| :---: | :---: | :---: | :---: | :---: |
| 57 | uniform convergence and continuity | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 58 | uniform convergence and continuity | Lecture, Group Problem Solving | Discussion, | CO3 |
| 59 | uniform convergence and integration | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 60 | uniform convergence and integration | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 61 | uniform convergence and integration | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 62 | uniform convergence and differentiation | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 63 | uniform convergence and differentiation | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 64 | uniform convergence and differentiation | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 65 | uniform convergence and differentiation | Lecture, Group Problem Solving | Discussion, | CO 3 |
| 66 | the Stone-Weierstrass theorem (without proof) | Lecture, Group Problem Solving | Discussion, | CO 3 |


| 67 | Power series | Lecture, Group Problem Solving | Discussion, | CO 4 |
| :---: | :---: | :---: | :---: | :---: |
| 68 | the exponential and logarithmic functions | Lecture, Group Problem Solving | Discussion, | CO 4 |
| 69 | the exponential and logarithmic functions | Lecture, Group Problem Solving | Discussion, | CO 4 |
| 70 | the trigonometric functions | Lecture, Group Problem Solving | Discussion, | CO 4 |
| 71 | the algebraic completeness of complex field | Lecture, Group Problem Solving | Discussion, | CO 4 |
| 72 | Fourier series. | Lecture, Group Problem Solving | Discussion, | CO 4 |
| 73 | Revision | Group Discussion |  |  |
| 74 | Revision | Group Discussion |  |  |
| 75 | Revision | Group Discussion |  |  |

ASSIGNMENTS/EXERCISES - Details \& Guidelines

|  | Date of submission/completion | Topic of Assignment \& Nature of assignment (Individual/Group Written/Presentation Graded or Non-graded etc) | Course Outcome |
| :---: | :---: | :---: | :---: |
| 1. | 12 March 2019 | Problems on Real analysis | CO2/CO3 |

Text Books:

1. Tom Apostol, Mathematical Analysis (second edition), Narosa Publishing House.
2. Walter Rudin, Principles of Mathematical Analysis (Third edition), International Student Edition.

## Additional Reading List

1.Royden H.L, Real Analysis, 2nd edition, Macmillan, New York.
2. Bartle R.G, The Elements of Real Analysis, John Wiley and Sons.
3. S.C. Malik, Savitha Arora, Mathematical Analysis, New Age International Ltd.
4. Edwin Hewitt, Karl Stromberg, Real and Abstract Analysis, Springer International, 1978.

