# SACRED HEART COLLEGE (AUTONOMOUS) 

Department of Mathematics
M.Sc. Mathematics

Course plan

Academic Year 2016-17

Semester 3

## COURSE PLAN COURSE: MULTIVARIATE CALCULUS AND INTEGRAL TRANSFORMS

Course Instructors
Prof. Sanil Jose

## Course Prerequisites:

Calculus, Analysis, Partial differentiation

## Guidelines/Suggestions for Teaching Methods and Student Learning Activities:

This course is taught as a lecture course with student participation and use of computers

## Course Objectives:

- To develop an idea about Fourier series and Fourier transforms
- To learn about directional derivatives and chain rule
- To study the idea of differentiation in multi variable functions
- To learn how integration is introduced in multi variable functions


## Text Books

Text 1: Tom APOSTOL, Mathematical Analysis, Second edition, Narosa Publishing House. Text 2: WALTER RUDIN, Principles of Mathematical Analysis, Third edition - International Student Edition.

|  | TOPIC |
| ---: | :--- |
| 1 | INTRODUCTION |
| 2 | THE WEIRSTRASS THEOREM |
| 3 | OTHER FORMS OF FOURIER SERIES |
| 4 | THE FOURIER INTEGRAL THEOREM |
| 5 | THE EXPONENTIAL FORM OF FORIER SERIES |
| 6 | INTEGRAL TRANSFORMS |
| 7 | CONVOLUTION |
| 8 | SEMINAR |
| 9 | SEMINAR |
| 10 | PROBLEMS |
| 11 | PROBLEMS |
| 12 | TUTORIAL |
| 13 | SEMINAR |
| 14 | QUESTION PAPER REVISION |
| 15 | THE DIRECTIONAL DERIVATIVE |
| 16 | CONTINUITY |
| 17 | TOTAL DERIVATIVE |


| 18 | TOTAL DERIVATIVE AS PARTIAL DERIVATIVES |
| :---: | :---: |
| 19 | TOTAL DERIVATIVE AS PARTIAL DERIVATIVES |
| 20 | APPLICATION TO COMPLEX NUMBERS |
| 21 | APPLICATION TO COMPLEX NUMBERS |
| 22 | MATRIX FORM |
| 23 | MATRIX FORM |
| 24 | JACOBIAN MATRIX |
| 25 | CHAIN RULE MATRIX FORM |
| 26 | CHAIN RULE MATRIX FORM |
| 27 | SEMINAR |
| 28 | SEMINAR |
| 29 | PROBLEMS |
| 30 | PROBLEMS |
| 31 | TUTORIAL |
| 32 | MEAN VALUE THEOREM |
| 33 | MEAN VALUE THEOREM |
| 34 | SUCCIFIENT CONDITION FOR DIFFERENTIABILITY |
| 35 | SUCCIFIENT CONDITION FOR DIFFERENTIABILITY |
| 36 | MIXED DERIVATIVE THEOREM |
| 37 | INVERSE FUNCTION THEOREM |
| 38 | IMPLICIT FUNCTION THEOREM |
| 39 | EXTREMA OF REAL VALUED FUNCTIONS |
| 40 | EXTREMA OF REAL VALUED FUNCTIONS |
| 41 | SEMINAR |
| 42 | SEMINAR |
| 43 | PROBLEMS |
| 44 | PROBLEMS |
| 45 | TUTORIAL |
| 46 | SEMINAR |
| 47 | SEMINAR |
| 48 | SEMINAR |
| 49 | SEMINAR |
| 50 | SEMINAR |
| 51 | SEMINAR |
| 52 | SEMINAR |
| 53 | SEMINAR |
| 54 | SEMINAR |
| 55 | PRIMITIVE MAPPING |
| 56 | PARTITION OF UNITY |
| 57 | PARTITION OF UNITY |
| 58 | CHANGE OF VARIABLES |
| 59 | DIFFERENTIAL FORMS |
| 60 | STOKES THEOREM |
| 61 | STOKES THEOREM |


| 62 | STOKES THEOREM |
| ---: | :--- |
| 63 | SEMINAR |
| 64 | SEMINAR |
| 65 | SEMINAR |
| 66 | SEMINAR |
| 67 | SEMINAR |
| 68 | SEMINAR |
| 69 | SEMINAR |
| 70 | SEMINAR |
| 71 | SEMINAR |
| 72 | SEMINAR |

References:-

1. Limaye Balmohan Vishnu, Multivariate Analysis, Springer.
2. Satish Shirali and Harikrishnan, Multivariable Analysis, Springer

## COURSE PLAN FOR FUNCTIONAL ANALYSIS

## Text book :Introductory Functional Analysis with applications <br> Author: ERWIN KREYSZIG,Wiley Classic Library Edition Published 1989 <br> Course objectives

1.Students will have a better perspective on mathematics as per modern requirement.
2.Students enhance their logical ,reasoning , analytical and problem solving skills. 3.The students possess an ethical view of life, and have a broader perspective transcending the provincial outlook.
4.Students are able to effectively communicate the knowledge of their study and research in their respective disciplines to their employers and to the society at large.
5.The students possess a passion for exploring new knowledge independently for the development of the nation and the world and are able to engage in a lifelong learning process.
6.To understand the basics of Functional analysis
7.To apply Functional analysis in the other disciplines.
8.To understand theory of Operators and Functionals using Linear Algebra.
9.To discover the link of Functional analysis with geometry , differential equations etc.

| SI.No | No. of <br> Sessions/hrs | Topics to be taught | Method of teaching |
| :--- | :--- | :--- | :--- |
| 1 | 1 | Fundamentals of Linear <br> Algebra and Metric spaces. | Lecture, Seminar, Assignment |
| 2. | 3 | Normed space and Banach <br> space, examples and their <br> properties, problems. | Lecture, assignment |
| 3 | 2 | Finite dimensional normed <br> spaces and their sub spaces <br> ,problems. | Lecture |
| 4 | 2 | Compactness and finite <br> dimension, problems. | Lecture |


| 5 | 2 | Linear operators, examples and their properties, problems. | Lecture, assignment |
| :---: | :---: | :---: | :---: |
| 6 |  | Test paper. |  |
| 7 | 2 | Bounded and continuous linear operators and examples. | Lecture |
| 8 | 2 | Problems based on bounded linear operators. | Lecture |
| 9 | 1 | Linear functionals, examples. | Lecture |
| 10 |  | First internal |  |
| 11 | 2 | Bounded linear Functionals and their properties, problems. | Lecture |
| 12 | 2 | Linear Operators and Functionals on a finite dimensional normed space, problems. | Lecture, assignment |
| 13 | 2 | Normed space of Operators and Functionals. | Lecture, assignment |
| 14 | 2 | Examples of dual spaces. | Lecture |
| 15 |  | Test paper on module 2 |  |


| 16 | 2 | Inner product spaces and <br> Hilbert spaces, examples, <br> problems. | Lecture |
| :--- | :--- | :--- | :--- |
| 17 | 2 | Further properties of inner <br> product spaces. | Lecture, seminar |
| 18 | 2 | Orthogonal complement <br> and direct sum , problems. | Lecture |
| 19 | 2 | 2 | Orthogonal sets and <br> sequences. |
| 21 | 2 | Bessel inequality, Gram- <br> Schmidt process for ortho <br> normalisation. | Lecture, seminar |
| 22 | 2 | Total ortho normal sets and <br> sequences, problems. | Lecture, seminar, assignment |
| 24 | 3 | 2 | Rieszs theorem . seminar <br> 25 2 |


| 2 | 3 | Problems based on Hilbert adjoint operators. | Lecture, assignment , seminar |
| :---: | :---: | :---: | :---: |
| 27 | 2 | Self adjoint, normal and unitary operators, problems. | Lecture, assignment |
| 28 |  | Test paper on module 3. |  |
| 29 | 2 | Zorns Lemma and its applications. | Lecture |
| 30 | 2 | Hahn Banach theorem for real vector space. | Lecture |
| 31 | 2 | Generalised Hahn Banach theorem, problems. | Lecture, assignment |
| 32 | 1 | Hahn Banach theorem for a normed space. | Lecture |
| 33 | 3 | Problems on Hahn Banach theorems | Lecture, seminar |


| 34 | 1 | Adjoint operator, relation <br> between adjoint operator <br> and Hilbert adjoint. | Lecture |
| :--- | :--- | :--- | :--- |
| 35 | 2 | Reflexive spaces, canonical <br> mapping. | Lecture,seminar |
| 36 | 2 | Important theorems and <br> problems. | Lecture |
| 37 | 2 | Bairs category theorem, <br> Uniform boundedness <br> theorem. | Lecture, seminar assignment |
| 38 | 1 | Problems on Uniform <br> boundedness theorem | Lecture, assignment |
| 39 |  | Model examination |  |

COURSE PLAN
DIFFERENTIAL GEOMETRY

## Course Teacher: Didimos K. V.

## COURSE OBJECTIVES

To understand the geometry of $n$-dimension Euclidean space.

## Text Book

1. Text Book: John A. Thorpe, Elementary Topics in Differential Geometry

| No of Hours | Topic | Method | Remarks/Reference |
| :---: | :---: | :---: | :---: |
| 2 | Graphs and level sets | Lecture, Group Discussion, Problem SolvingLecture | Module-1 <br> (20 Hours) |
| 2 | vector fields | Lecture, Group Discussion, Problem Solving |  |
| 4 | The tangent space | Lecture, Group Discussion, Problem Solving |  |
| 6 | Surfaces | Lecture, Group Discussion, Problem Solving |  |
| 6 | Vector fields on surfaces, orientation. | Lecture, Group Discussion, Problem Solving |  |
| 4 | The Gauss map | Lecture, Group Discussion, Problem Solving | Module-II <br> (15 Hours) |
| 5 | Geodesics | Lecture, Group Discussion, Problem Solving |  |
| 6 | Parallel transport | Lecture, Group Discussion, Problem Solving |  |
| 6 | The Weingarten map | Lecture, Group Discussion, Problem Solving | Module-III <br> (20 Hours) |
| 7 | Curvature of plane curves | Lecture, Group Discussion, Problem Solving |  |
| 7 | Arc length and line integrals | Lecture, Group Discussion, Problem Solving |  |


| 7 | Curvature of surfaces | Lecture, Group Discussion, <br> Problem Solving |  |
| :---: | :--- | :--- | :--- |
| 7 | Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving | Module-IV <br> (20 Hours) |
| 6 | local equivalence of <br> surfaces and Parametrized surfaces | Lecture, Group Discussion, <br> Problem Solving |  |

## References:-

1. Serge Lang, Differential Manifolds
2. I.M. Siger, J.A Thorpe, Lecture notes on Elementary topology and Geometry, Springer (1967)
3. S. Sternberg, Lectures on Differential Geometry, Prentice-Hall, 1964.
4. M. DoCarmo, Differential Geometry of curves and surfaces.
5. Goursat, Mathematical Analysis, Vol - 1(last two chapters)

## COURSE PLAN <br> NUMBER THEORY

## Course Teacher: Didimos K. V.

## COURSE OBJECTIVES

To understand arithmetic functions, prime number theorm.
To understand algebraic integers in a number field and factorization of ideals.

## Text Book

1. Introduction to Analytic Number Theory, Tom M Apostol, Springer International Student Edition.
2. Algebraic Number Theory and Fermat's Last Theorem, Ian Stewart and David Tall, Third Edition.

| No of <br> Hours | Topic | Method | Remarks/Reference |
| :---: | :--- | :--- | :--- |
| 1 | The Mobius function, The Euler totient <br> function | Lecture, Group <br> Discussion, Problem <br> SolvingLecture |  |
| 2 | The Dirichlet product of arithmetical <br> functions, Dirichlet inverses and Mobius <br> inversion formula | Lecture, Group <br> Discussion, Problem <br> Solving |  |
| 2 | The Mangoldt function <br> Multiplicative functions and Dirichlet <br> multiplication | Lecture, Group <br> Discussion, Problem <br> Solving | Module-1 |
| 2 | The inverse of completely multiplicative <br> functions | Lecture, Group <br> Discussion, Problem <br> Solving |  |
| 3 | The Liovillie's function ,The divisor <br> function, Generalized convolutions |  |  |
| 1 | The big oh notation, Asymptotic equality <br> of functions | Lecture, Group <br> Discussion, Problem <br> Solving |  |


| 3 | Euler's summation formula, Some elementary asymptotic formulas | Lecture, Group Discussion, Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 3 | The average order of $\mathrm{d}(\mathrm{n})$, The average order of the divisor function, Average order of $\phi(n)$ | Lecture, Group Discussion, Problem Solving |  |
| 1 | An application of distribution of lattice points visible from the origin | Lecture, Group <br> Discussion, Problem Solving |  |
| 2 | Averageorder of $\mu(\mathrm{n})$ and of $\Lambda(\mathrm{n})$ | Lecture, Group Discussion, Problem Solving |  |
| 2 | The partial sums of a Dirichlet product | Lecture, Group Discussion, Problem Solving |  |
| 3 | Application to $\mu(\mathrm{n})$ and $\Lambda(\mathrm{n})$ | Lecture, Group Discussion, Problem Solving |  |
| 1 | Chebyshev's functions $\Psi(x)$ and $\theta(x)$ | Lecture, Group Discussion, Problem Solving |  |
| 1 | Relation connecting $\Psi(x)$ and $\pi(\mathrm{x})$ | Lecture, Group Discussion, Problem Solving |  |
| 2 | Some equivalent forms of prime number theorem | Lecture, Group <br> Discussion, Problem Solving | Module-2 |
| 2 | Inequalities of $\pi(n)$ and $p_{n}$ | Lecture, Group Discussion, Problem Solving | (18 Hours) |
| 2 | Definition and basic properties of congruences | Lecture, Group Discussion, Problem Solving |  |
| 1 | residue classes and complete residue systems | Lecture, Group Discussion, Problem Solving |  |


| 1 | liner congruences | Lecture, Group Discussion, Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 2 | Reduced residue systems and Euler Fermat theorem | Lecture, Group Discussion, Problem Solving |  |
| 1 | Polynomial congruences modulo | Lecture, Group Discussion, Problem Solving |  |
| 3 | Lagrange's theorem, applications of Lagrange's theorem | Lecture, Group Discussion, Problem Solving |  |
| 1 | Simultaneous linear congruences | Lecture, Group Discussion, Problem Solving |  |
| 1 | The Chinese reminder theorem. | Lecture, Group Discussion, Problem Solving |  |
| 2 | Trivial FactorizationsFactorization into Irreducibles | Lecture, Group Discussion, Problem Solving |  |
| 3 | Examples of Non-Unique Factorization into Irreducibles | Lecture, Group Discussion, Problem Solving |  |
| 4 | Prime Factorization | Lecture, Group Discussion, Problem Solving | Module-3 <br> (17 Hours) |
| 5 | Euclidean Domains | Lecture, Group Discussion, Problem Solving |  |
| 3 | Euclidean Quadratic Fields. | Lecture, Group Discussion, Problem Solving |  |
| 6 | Prime Factorization of Ideals | Lecture, Group Discussion, Problem Solving | Module-4 <br> (15 Hours) |


| 6 | The Norm of an Ideal | Lecture, Group <br> Discussion, Problem <br> Solving |
| :---: | :--- | :--- |
| 3 | Nonunique Factorization of Cyclotomic <br> Fields. | Lecture, Group <br> Discussion, Problem <br> Solving |

1. Additional Reading List
2. Hardy G.H and Wright E.M, Introduction to the Theory of numbers, Oxford, 1981
3. Leveque W.J, Topics in Number Theory, Addison Wesley, 1961.
4. J.P Serre, A Course in Arithmetic, GTM Vol. 7, Springer-Verlag, 1973
5. D Marcus, Number Fields (Springer-Verlag, New York-Heidelberg)
