# SACRED HEART COLLEGE (AUTONOMOUS) 

Department of Mathematics

## BACHELOR OF SCIENCE [MATHEMATICS]

## Course plan

Academic Year 2016-17

Semester 6

## COURSE PLAN

U6CRMATO9 : REAL ANALYSIS

## COURSE OBJECTIVE

*To study elementary concepts of real analysis

* To equip the students for analysing a problem and solving it.
*To understand both algebraic and geometrical implications of the results in real analysis.


## TEXT BOOK

*S.C.MALIK SAVITHA ARORA ... MATHEMATICAL ANALYSIS , SECOND EDITION

| Sessions | Topic | Method | Remarks/Reference |
| :---: | :---: | :---: | :---: |
| 1 | Introductory Session |  |  |
| 2 | A necessary condition for convergence | Lecture,Group Discussion, Problem Solving |  |
| 3 | Cauchy's general principle of convergence for a series. | Lecture,Group Discussion, Problem Solving |  |
| 4 | Positive term series. | Lecture,Group Discussion, Problem Solving |  |
| 5 | A necessary condition for convergence of positive term series. | Lecture,Group Discussion, Problem Solving |  |
| 6 | Geometric series. | Lecture,Group Discussion, Problem Solving |  |
| 7 | The comparison series $\sum 1 / \mathrm{n}^{\mathrm{p}}$ Comparison test for positive term series without proof. | Lecture,Group Discussion, Problem Solving |  |
| 8 | Cauchy's root test | Lecture,Group Discussion, Problem Solving |  |
| 9 | DALEMBERTE'S Ratio test | Lecture,Group Discussion, Problem Solving |  |
| 10 | Raabe's test. | Lecture,Group Discussion, Problem Solving |  |
| 11 | Gauss's test. | Lecture,Group Discussion, Problem Solving |  |


| 12 | Series with arbitrary terms. Alternating series. | Lecture,Group Discussion, Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 13 | Absolute convergence | Lecture,Group Discussion, Problem Solving |  |
| 14 | Solving Exercise Problems |  |  |
| 15 | Test paper 1 |  |  |
| 16 | Introduction to continuous function | Lecture, Group Discussion |  |
| 17 | Continuity at a point | Lecture, Group Discussion |  |
| 18 | Continuity in an interval | Lecture,Group Discussion, Problem Solving |  |
| 19 | Discontinuous functions | Lecture,Group Discussion, Problem Solving |  |
| 20 | Theorems on continuity | Lecture |  |
| 21 | More Theorems | Lecture |  |
| 22 | Theorems on continuity | Lecture |  |
| 23 | Functions continuous on closed intervals | Lecture,Group Discussion, Problem Solving |  |
| 24 | Functions continuous on closed intervals | Lecture,Group Discussion, Problem Solving |  |
| 25 | Functions continuous on closed intervals | Lecture,Group Discussion, Problem Solving |  |
| 26 | Uniform continuity | Lecture,Group Discussion, Problem Solving |  |
| 27 | Uniform continuity | Lecture,Group Discussion, Problem Solving |  |
| 28 | Doubt Clearing |  |  |
| 29 | Revision on module 2 |  |  |
| 30 | Test Paper 2 |  |  |
| 31 | Introduction of module 3 | Lecture and Group Discussion |  |


| 32 | Definiton and existence of the integral | Lecture,Group Discussion, Problem Solving |  |
| :---: | :---: | :---: | :---: |
| 33 | Definiton and existence of the integral | Lecture,Group Discussion, Problem Solving |  |
| 34 | Inequalities of integrals | Lecture,Group Discussion, Problem Solving |  |
| 35 | Refinement of partitions of integrability | Lecture,Group Discussion, Problem Solving |  |
| 36 | Darboux's theorem | Lecture |  |
| 37 | Condition of integrability | Lecture |  |
| 38 | Integrability of the sum of integrable functions | Lecture, Problem Solving |  |
| 39 | Integrability of the sum of integrable functions | Lecture, Problem Solving |  |
| 40 | Integrability of the sum of integrable functions | Lecture,Problem Solving |  |
| 41 | Integrability of the sum of integrable functions | Lecture, Problem Solving |  |
| 42 | Integrability of the sum of integrable functions | Lecture,Problem Solving |  |
| 43 | Group Discussion and doubt clearing |  |  |
| 44 | The integrals as the limit of a sum | Lecture,Group Discussion, Problem Solving |  |
| 45 | The integrals as the limit of a sum | Lecture,Group Discussion, Problem Solving |  |
| 46 | Some applications | Lecture,Group Discussion, Problem Solving |  |
| 47 | Some integrable functions | Lecture,Group Discussion, Problem Solving |  |
| 48 | Some integrable functions | Lecture,Group Discussion, Problem Solving |  |
| 49 | Integration and Differentiation | Lecture,Group Discussion, Problem Solving |  |
| 50 | The fundamental theorem of calculus | Lecture,Group Discussion, Problem Solving |  |
| 52 | Revision of module 3 |  |  |

| 52 | Test Paper 3 |  |  |
| :---: | :---: | :---: | :---: |
| 53 | Introduction to module 4 |  |  |
| 54 | Point wise convergence. | Lecture, Group Discussion |  |
| 55 | Examples for Point wise convergence | Group Discussion |  |
| 56 | Uniform convergence on an interval | Lecture,Group Discussion, Problem Solving |  |
| 57 | Uniform convergence on an interval | Problem Solving |  |
| 58 | Cauchy`s criterion for uniform convergence | Lecture,Group Discussion, Problem Solving |  |
| 59 | Solved examples |  |  |
| 60 | Examples | Group Discussion |  |
| 61 | A test for uniform convergence of sequences | Lecture,Group Discussion, Problem Solving |  |
| 62 | A test for uniform convergence of sequences | Lecture, Group Discussion |  |
| 63 | Problems on test for Uniform convergence of sequences | Group Discussion |  |
| 64 | Test for uniform convergence of series | Lecture, Group Discussion |  |
| 65 | Test for uniform convergence of series | Lecture, Group Discussion |  |
| 66 | Problems on test for Uniform convergence of series | Group Discussion |  |
| 67 | Weierstrass M test | Lecture, Group Discussion |  |
| 68 | Examples | Lecture,Group Discussion, Problem Solving |  |
| 69 | Abel's test | Lecture,Group Discussion, Problem Solving |  |
| 70 | Examples | Lecture,Group Discussion, Problem Solving |  |
| 71 | Statement of Dirichelet's test without proof. | Lecture,Group Discussion, Problem Solving |  |
| 72 | Solving Problems |  |  |
| 73 | Doubt Clearing |  |  |
| 74 | Revision | Lecture, Group Discussion, Problem Solving |  |
| 75 | Test Paper 4 |  |  |

## Course Plan

## U6CRMAT10 - Complex Analysis

## Course Objectives:

The objectives of the course include familiarising the student with the theory of functions of one complex variable, differentiability and analyticity of such functions, complex integration and related topics

| Day | Topic | Method |
| :--- | :--- | :--- |
|  | MODULE I BEGINS |  |
| 1 | Functions of a complex variable | Lecture |
| 2 | Selected Exercises on Pages 37-38 | Seminar |
| 3 | Limits | Lecture |
| 4 | Theorems on Limits | Lecture |
| 5 | Continuity | Lecture |
| 6 | Selected Exercises on Pages 55-56 | Seminar |
| 7 | Derivatives | Lecture |
| 8 | Selferentiation Formulas | Lecture |
| 9 | Cauchy- Remann Equations | Lecture |
| 10 | Sufficient Conditions for Differentiability | Lecture |
| 11 | Selected exercises on Pages 71,72 and 73 | Assignment |
| 12 | Analytic Functions | Lecture |
| 13 | Examples of Analytic FunctionsLecture | Lecture |
| 14 | Selected Exercises on Pages 77-78 | Exercise |
| 15 | Harmonic Functions | Lecture |
| 16 | Harmonic Functions ( Continued ) | Lecture |
| 17 | Selected Exercises on pages 81-82 | Seminar |
| 18 | The Exponential Function | Lecture |
| 19 | Selected Exercises on pages 92-93 | Seminar |
| 20 | The Logarithm Function | Lecture |
| 21 | Selected Exercises on pages 97-98 | Seminar |
| 22 | 23 |  |


| 24 | Complex Exponents | Lecture |
| :---: | :---: | :---: |
| 25 | Complex Exponents (Continued) | Lecture |
| 26 | Selected Exercises on Page 104 | Seminar |
| 27 | Trigonometric Functions | Lecture |
| 28 | Selected Exercises on Pages 108-109 | Seminar |
| 29 | Hyperbolic Functions | Lecture |
| 30 | Selected Exercises on Pages 111-112 | Seminar |
| 31 | Inverse Trigonometric and Hyperbolic Functions | Lecture |
| 32 | Selected Exercises on Pages 114-115 | Seminar |
| 33 | FIRST CIA |  |
|  | (MODULE II BEGINS) |  |
| 34 | Derivatives of Functions | Lecture |
| 35 | Definite Integrals of Functions | Lecture |
| 36 | Selected Exercises on Pages 121 | Assignment |
| 37 | Contours | Lecture |
| 38 | Contours ( Continued) | Lecture |
| 39 | Selected Exercises on pages 125-126 | Seminar |
| 40 | Contour Integrals | Lecture |
| 41 | Some Examples of Contour Integrals | Lecture |
| 42 | Upper Bounds for Moduli of Contour integrals | Lecture |
| 43 | Examples and Selected Exercises on pages 141 | Seminar |
| 44 | Antiderivatives | Lecture |
| 45 | Cauchy Goursat Theorem | Lecture |
| 46 | Simply Connected Domains | Lecture |
| 48 | Multiply Connected Domains | Lecture |
| 49 | Selected Exercises on Pages 160,161 \& 162 | Assignment |
| 50 | Cauchy's Integral Formula | Lecture |
| 51 | An extension of Cauchy's Integral Formula | Lecture |
| 52 | Some Consequences of the Extension | Lecture |
| 53 | Selected Exercises on pages 171-172 | Seminar |
| 54 | Liouville's Theorem and the Fundamental theorem of Algebra | Lecture |
| 55 | Maximum Modulus Principle | Lecture |


|  | (MODULE III BEGINS) |  |
| :---: | :---: | :---: |
| 56 | Convergence of Sequences | Lecture |
| 56 | Convergence of Series | Lecture |
| 57 | Convergence of Series (Continued) | Lecture |
| 58 | Selected Exercises on Pages 188-189 | Assignment |
| 59 | Taylor Series | Lecture |
| 60 | Proof of Taylor's theorem | Lecture |
| 61 | Examples of Taylor's series | Lecture |
| 62 | Selected Exercises on pages 196-197 | Seminar |
| 63 | Laurent Series | Lecture |
| 64 | Examples of Laurent Series | Lecture |
| 65 | Selected Exercises on pages 205-207 | Assignment |
| 66 | SECOND CIA | Lecture |
|  | MODULE IV BEGINS | Lecture |
| 67 | Isolated Singular Points | Lecture |
| 68 | Residues | Lecture |
| 69 | Examples | Lecture |
| 70 | Cauchy's Residue Theorem | Lecture |
| 71 | Selected Exercises on pages 239-240 | Seminar |
| 72 | The three types of isolated singular points | Lecture |
| 73 | Examples | Lecture |
| 74 | Selected Exercises on pages 243-244 | Assignment |
| 75 | Residues at Poles | Lecture |
| 76 | Examples | Lecture |
| 77 | Selected Exercises on pages 248-249 | Seminar |
| 78 | Evaluation of improper integrals | Lecture |
| 79 | Evaluation of improper integrals ( Continued) | Lecture |
| 80 | Examples | Lecture |
| 81 | Selected Exercises on pages 267-268 | Seminar |
| 82 | Improper integrals from Fourier Analysis | Lecture |
| 83 | Improper integrals from Fourier Analysis (Continued) | Lecture |
| 84 | Jordan's Lemma | Lecture |


| 85 | Selected Exercises on Pages 275-276 | Seminar |
| :--- | :--- | :--- |
| 86 | Definite Integrals involving Sines and Cosines | Lecture |
| 87 | Selected Exercises on Pages 290-291 | Assignment |
| 88 | REVISION | Lecture |
| 89 | REVISION | Lecture |
| 90 | REVISION | Lecture |

## COURSE PLAN

## U6CRMAT11:DISCRETE MATHEMATICS

Course Objectives: * To introduce graph theory and its applications To understand cryptography *To study lattices.

| Sessions | Topic | Remarks/Reference |
| :---: | :---: | :---: |
| 1 | Introduction to Graph |  |
| 2 | History |  |
| 3 | Definition and examples |  |
| 4 | Graph as models |  |
| 5 | More Definitions |  |
| 6 | Examples |  |
| 7 | Vertex degree |  |
| 8 | Examples and problems |  |
| 9 | Sub Graphs |  |
| 10 | Problems |  |
| 11 | Seminar |  |
| 12 | Seminar |  |
| 13 | Paths and cycles |  |
| 14 | Matrix representation |  |
| 15 | Problems |  |
| 16 | Seminar |  |
| 17 | Seminar |  |
| 18 | Trees. |  |
| 19 | connectivity. |  |
| 20 | Connectivity Problems |  |
| 21 | Connectivity Problems |  |
| 22 | Properties of connected graphs |  |
| 23 | Properties of connected graphs |  |
| 24 | Bridges. |  |
| 25 | Bridges |  |
| 26 | Spanning trees |  |
| 27 | Cut vertices |  |
| 28 | Cut vertices problems |  |
| 29 | Cut vertices problems |  |
| 30 | Revision |  |
| 31 | Problems |  |
| 32 | Class test |  |
| 33 | Euler Tour |  |
| 34 | Problems |  |
| 35 | Problems |  |
| 36 | Hamiltonian Cycle |  |
| 37 | Problems |  |


| 38 | Euler's tour |  |
| :---: | :---: | :---: |
| 39 | Chinese postman problem |  |
| 40 | Hamiltonian Graphs |  |
| 41 | Examples and problems |  |
| 42 | Examples and problems |  |
| 43 | Examples and problems |  |
| 44 | Matching |  |
| 45 | Matching |  |
| 46 | Matching |  |
| 47 | Hall's marriage problem |  |
| 48 | Personal assignment problem |  |
| 49 | Optimal assignment Prroblem |  |
| 50 | Problems |  |
| 51 | Revision |  |
| 52 | Introduction |  |
| 53 | Caesar Cipher |  |
| 54 | Problems |  |
| 55 | Problems |  |
| 56 | Hill's Ciper |  |
| 57 | Problems |  |
| 58 | Problems |  |
| 59 | Public key Cryptography |  |
| 60 | Public key Cryptography |  |
| 61 | RSA Cryptosystem |  |
| 62 | Problems |  |
| 63 | Problems |  |
| 64 | the Knapsack problem |  |
| 65 | the Knapsack problem |  |
| 66 | test |  |
| 67 | Introduction |  |
| 68 | Diagramatical Representation of a Poset, Diagramatical Representation of a Poset, |  |
| 69 | Isomorphisms |  |
| 70 | Isomorphisms |  |
| 71 | Duality |  |
| 72 | Duality |  |
| 73 | Product of two Posets |  |
| 74 | Lattices |  |
| 75 | Lattices |  |
| 76 | Semilattices, |  |
| 77 | Complete Lattices, |  |
| 78 | Sublattices |  |
| 79 | Revision |  |
| 80 | Revision |  |

## COURSE PLAN <br> U6CRMAT12 : LINEAR ALGEBRA AND METRIC SPACES

Course Objectives: * To introduce vector spaces ,basis and linear transformation. To understand linear dependence and independence
*To study metric spaces and its properties.

## TEXT BOOK

* Richard Bronson, Gabriel B Costa - Linear Algebra An Introduction(Second Edition)
* G.F.Simmons - Introduction to topology and modern analysis(Tata Mc Graw Hill)

| Sessions | Topic | Method |
| :---: | :--- | :--- |
| 1 | Introductory Session | Interactive session |
| 2 | Definition of vector space | Lecture and interaction |
| 3 | Examples | Group discussion and problem solving |
| 4 | Solving exercise 2.1 |  |
| 5 | Theorems | Lecture |
| 6 | Subspaces-Definition | Lecture,Group Discussion |
| 7 | Examples | Group discussion and problem solving |
| 8 | Solving exercise 2.2 |  |
| 9 | Theorems | Lecture |
| 10 | Linear <br> independence | Lecture,Group Discussion |
| 11 | Problems | Group discussion and problem solving |
| 12 | Theorems | Lecture |
| 13 | Basis | Lecture |
| 14 | Examples | Group discussion and problem solving |
| 15 | Theorems | Lecture |
| 16 | Theorems | Lecture |
| 17 | Dimension of Vector space | Lecture |
| 18 | Coordinate representation | Lecture |
| 19 | Problems | Row space of a matrix |
| 20 |  |  |
| 10 Lecture |  |  |



| 49 | Test Paper 2 |  |
| :---: | :---: | :---: |
| 50 | Introduction to module 3 | Interaction session |
| 52 | Metric-Definition | Lecture,Group Discussion |
| 52 | Examples | Lecture,Group Discussion |
| 53 | Metric Space-Definition | Lecture,Group Discussion |
| 54 | Examples | Lecture,Group Discussion |
| 55 | More examples on metric spaces | Lecture,Group Discussion |
| 56 | Open set-Definition | Lecture,Group Discussion |
| 57 | Examples | Lecture,Group Discussion |
| 58 | Theorems | Lecture |
| 59 | Theorems | Lecture |
| 60 | Theorems | Lecture |
| 61 | Theorems | Lecture |
| 62 | Interior of a set and its properties | Lecture, Group Discussion |
| 63 | Closed set-Definition | Lecture and interaction |
| 64 | Examples | Lecture,Group Discussion |
| 65 | Theorems | Lecture |
| 66 | Theorems | Lecture |
| 67 | Cantor set | Lecture |
| 68 | Properties of cantor set | Lecture,Group Discussion |
| 69 | Boundary of a set and its properties | Lecture |
| 70 | Revision |  |
| 71 | Test Paper 3 |  |
| 72 | Introduction to module 4 | Interaction session |


| 73 | Convergence of a sequence | Lecture |
| :---: | :--- | :--- |
| 74 | Examples | Group discussion and problem solving |
| 75 | Theorems | Lecture |
| 76 | Cantor's Intersection Theorem | Lecture |
| 77 | Theorems | Lecture |
| 78 | Complete metric space | Lecture |
| 79 | Continuous mapping | Lecture |
| 80 | Theorems | Lecture |
| 81 | Theorems | Lecture |
| 82 | Theorems | Lecture |
| 83 | Theorems | Lecture |
| 84 | Revision |  |
| 85 | Test Paper 4 |  |

## Course Plan

## U6CRMAT13 - Operations Research

## COURSE OBJECTIVES

The course aims

* To introduce and explain the ideas relevant to Mathematical programming in detail;
* To explain methods to solve Linear Programming Problem


## Basic Reference

1. Optimization methods in Operations Research and System Analysis - K.V.Mital and C.Mohan
2. Operations Research - J.K.Sharma

| Sessions | Topic | Method |
| :--- | :--- | :--- |
| 1 | Mathematical Preliminaries <br> Introduction | Lecturing |
| 2 | Euclidean space | Lecturing |
| 3 | Convex sets | Lecturing |
| 4 | Convex sets | Lecturing |
| 5 | Convex sets | Lecturing |
| 6 | Introduction to LPP | Lecturing |
| 7 | LP in 2 dimensional space | Lecturing |
| 8 | Optimal solution | Lecturing |
| 9 | Simple Problems | Lecturing |
| 10 | Problems | Group work |
| 11 | Simplex method | Lecturing |
| 12 | Problems | Group work |


| 13 | Problems | Group work |
| :---: | :---: | :---: |
| 14 | 2 Phase simplex method | Lecturing |
| 15 | Big M method | Lecturing |
| 16 | Problems | Lecturing |
| 17 | Problems | Group work |
| 18 | Problems | Lecturing |
| 19 | Duality in LPP | Lecturing |
| 20 | Problems | Group work |
| 21 | CIA - I (Module -1) |  |
| 22 | Problems | Lecturing |
| 23 | Dual simplex method | Lecturing |
| 24 | Applications | Lecturing |
| 25 | Problems | Group work |
| 26 | Problems | Lecturing |
| 27 | Introduction Transportation Problem | Lecturing |
| 28 | Problems | Lecturing |
| 29 | Finding basic feasible solution | Lecturing |
| 30 | Testing of optimality | Lecturing |
| 31 | Loop in transportation | Lecturing |
| 32 | degeneracy | Lecturing |
|  | Problems | Lecturing |
| 33 | Unbalance Problem | Lecturing |
| 34 | Problems | Lecturing |
| 35 | Assignment Problems | Lecturing |
| 36 | Problems | Lecturing |
| 37 | Queueing theory introduction | Lecturing |
| 38 | Essential features of queuing system | Lecturing |
| 39 | Calling Population | Lecturing |


| 40 | Characteristics queuing process | Lecturing |
| :---: | :---: | :---: |
| 41 | Queue discipline | Lecturing |
| 42 | Service Process | Lecturing |
| 43 | Perfomance measure of system | Lecturing |
| 44 | Transient state, steady state | Lecturing |
| 45 | Relation amoung performance measure | Lecturing |
| 46 | Probability distribution in queuing system | Lecturing |
| 47 | Problems | Lecturing |
| 48 | Problrms | Lecturing |
| 49 | Problems | Lecturing |
| 50 | Problems | Lecturing |
| 51 | Distribution of arrival | Lecturing |
| 52 | Distribution of interarrival times | Lecturing |
| 53 | Distribution of departure | Lecturing |
| 54 | Distribution of service time | Lecturing |
| 55 | Convex hull | Lecturing |
| 56 | Vertices of a convex set | Lecturing |
| 57 | Convex polyhedron | Lecturing |
| 58 | Hyperplanes, half space and polytopes | Lecturing |
| 59 | Separating and supporting hyperplanes | Lecturing |
| 60 | Numerical examples | Lecturing |
| 61 | CIA II | 2 HOURS |
| 62-72 | Revision |  |

