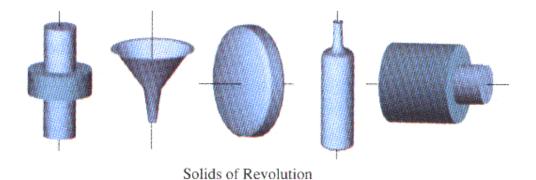
CALCULUS

VOLUME OF A SOLID OF REVOLUTION

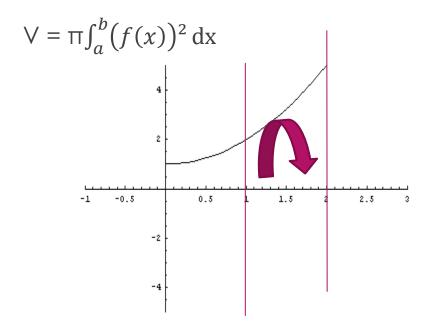
- DISC METHOD
- ►WASHER METHOD
- SHELL METHOD

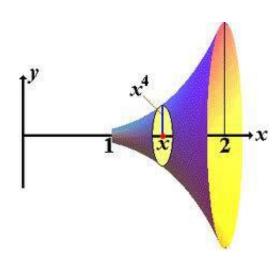
If a region in the plane is revolved about a given line, the resulting solid is a solid of revolution, and the line is called the axis of revolution.



DISC METHOD

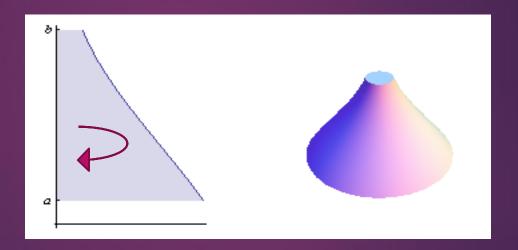
The volume of the solid generated by a region under f(x) bounded by the x-axis and vertical lines x=a and x=b, which is revolved **about the x-axis** is





The volume of the solid generated by a region under f(y) (to the left of f(y) bounded by the y-axis, and horizontal lines y=c and y=d which is revolved **about the y-axis**

$$V = \pi \int_{c}^{d} (f(y))^{2} dy$$

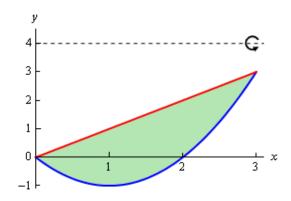


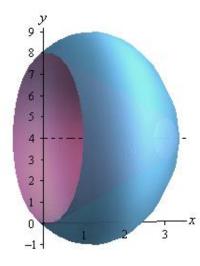
WASHER METHOD

This is an extension of the disc method.

► The volume of the solid generated by a region between f(x) and g(x) bounded by the vertical lines x=a and x=b, which is revolved about the x-axis is

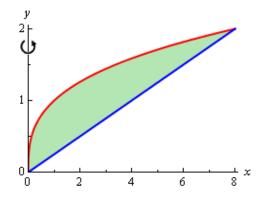
$$V = \pi \int_{a}^{b} \left| ((f(x))^{2} - (g(x))^{2} \right| dx$$

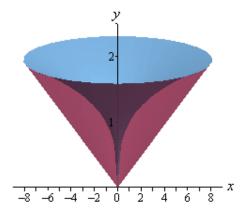




► The volume of the solid generated by a region between f(y) and g(y) bounded by the horizontal lines y=c and y=d which is revolved about the y-axis is

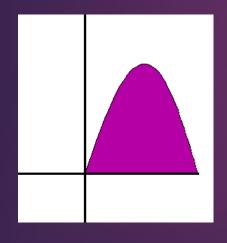
$$V = \pi \int_{c}^{d} \left| \left(f(y) \right)^{2} - (g(y))^{2} \right| dy$$

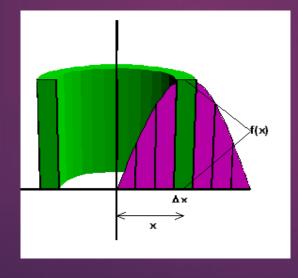


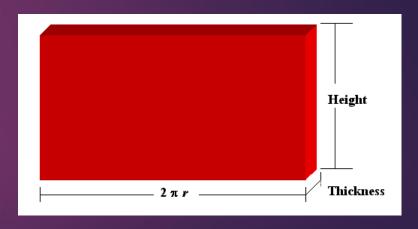


SHELL METHOD

The shell method is a method of calculating the volume of a solid of revolution when integrating along an axis parallel to the axis of revolution.







- The volume of the solid generated by a region bounded by the vertical lines x=a and x=b, which is revolved about the y-axis is $V = 2\pi \int_a^b x f(x) dx$
- The volume of the solid generated by a region bounded by the y-axis, and horizontal lines y=c and y=d which is revolved about the x-axis is

$$\vee = 2\pi \int_{c}^{d} y f(y) dy$$

THANK YOU