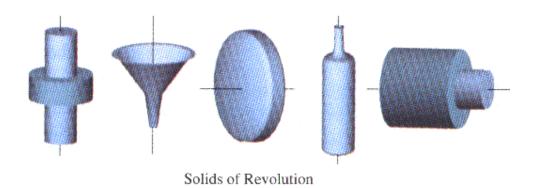
CALCULUS

VOLUME OF A SOLID OF REVOLUTION

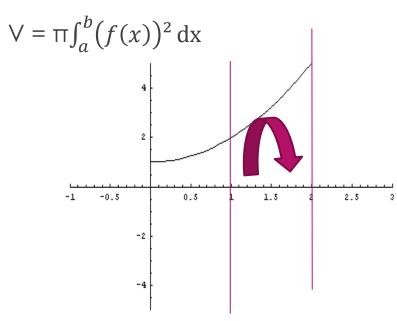
DISC METHOD
WASHER METHOD
SHELL METHOD

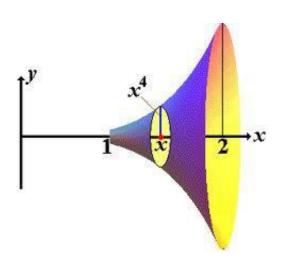
IF A REGION IN THE PLANE IS REVOLVED ABOUT A GIVEN LINE, THE RESULTING SOLID IS A SOLID OF REVOLUTION, AND THE LINE IS CALLED THE AXIS OF REVOLUTION.



DISC METHOD

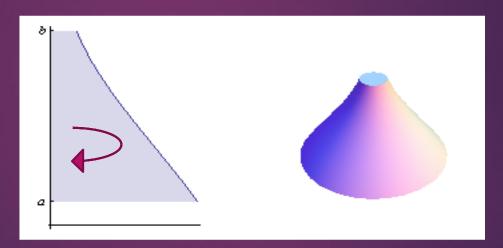
The volume of the solid generated by a region under f(x) bounded by the x-axis and vertical lines x=a and x=b, which is revolved **about the x-axis** is





The volume of the solid generated by a region under f(y) (to the left of f(y) bounded by the y-axis, and horizontal lines y=c and y=d which is revolved **about the y-axis**

 $V = \pi \int_{c}^{d} (f(y))^{2} dy$

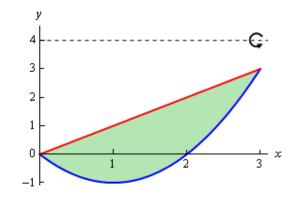


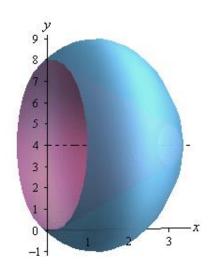


This is an extension of the disc method.

The volume of the solid generated by a region between f(x) and g(x) bounded by the vertical lines x=a and x=b, which is revolved about the x-axis is

$$V = \pi \int_{a}^{b} |((f(x))^{2} - (g(x))^{2})| dx$$

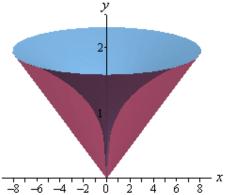






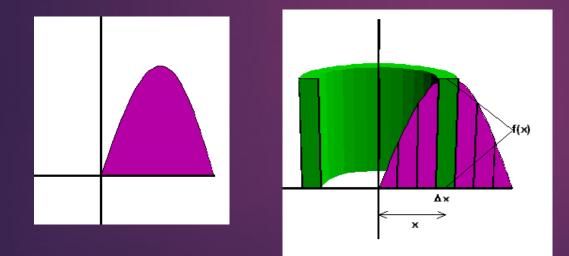
The volume of the solid generated by a region between f(y) and g(y) bounded by the horizontal lines y=c and y=d which is revolved about the y-axis is

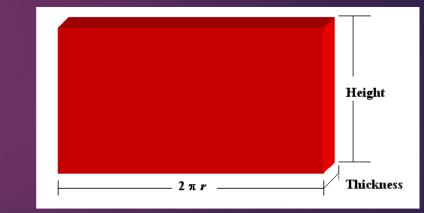
$$\bigvee = \pi \int_{c}^{d} \left| \left(f(y) \right)^{2} - (g(y))^{2} \right| dy$$



SHELL METHOD

The shell method is a method of calculating the volume of a solid of revolution when integrating along an axis parallel to the axis of revolution.







The volume of the solid generated by a region bounded by the vertical lines x=a and x=b, which is revolved about the y-axis is $V = 2\pi \int_{a}^{b} xf(x)dx$

The volume of the solid generated by a region bounded by the yaxis, and horizontal lines y=c and y=d which is revolved about the x-axis is

 $\bigvee = 2\pi \int_{c}^{d} y f(y) dy$



THANK YOU